

# Effects of Vegetation on Stream Systems

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# Examples of Aquatic Vegetation



Willow. <http://www.naturalheritage.state.pa.us>



Reed canary-grass. <http://www.naturalheritage.state.pa.us>



Floodplain forest. <http://www.nrcs.usda.gov>



Floodplain forest.  
<http://www.nature.org>

# **Model of Wu and Wang (2004) and Wu et al. (2005)**

# 2-D Depth-av. Flow Eqn. with Vegetation Effects

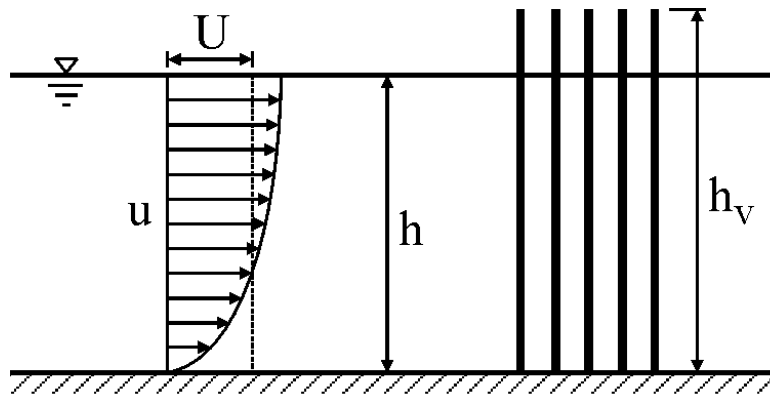
$$\frac{\partial[\rho(1-c)h]}{\partial t} + \frac{\partial[\rho(1-c)Uh]}{\partial x} + \frac{\partial[\rho(1-c)Vh]}{\partial y} = 0$$

$$\begin{aligned} & \frac{\partial[\rho(1-c)Uh]}{\partial t} + \frac{\partial[\rho(1-c)UUh]}{\partial x} + \frac{\partial[\rho(1-c)UVh]}{\partial y} \\ & = -\rho g(1-c)h \frac{\partial z_s}{\partial x} + \frac{\partial(hT_{xx})}{\partial x} + \frac{\partial(hT_{xy})}{\partial y} - \tau_{bx} - f_{dx}h \end{aligned}$$

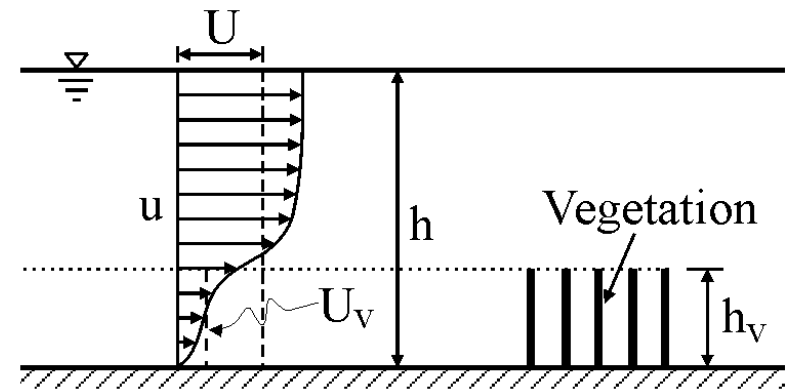
$$\begin{aligned} & \frac{\partial[\rho(1-c)Vh]}{\partial t} + \frac{\partial[\rho(1-c)UVh]}{\partial x} + \frac{\partial[\rho(1-c)VVh]}{\partial y} \\ & = -\rho g(1-c)h \frac{\partial z_s}{\partial y} + \frac{\partial(hT_{yx})}{\partial x} + \frac{\partial(hT_{yy})}{\partial y} - \tau_{by} - f_{dy}h \end{aligned}$$

( $c$  = vegetation density)

# Modeling of Vegetation Effects



(a). Emergent



(b). Submerged

## Drag and inertia forces:

$$\vec{F} = \frac{1}{2} C_D \rho N_v A_v |U_v| \vec{U}_v + \rho C_M N_v V_v \frac{\partial \vec{U}_v}{\partial t}$$

For submerged vegetation (Stone and Shen 2002):

$$\vec{U}_v = \eta_v \vec{U} \left( \frac{h_v}{h} \right)^{1/2}$$

$h_v$  = vegetation height, and  $\eta_v$  = coefficient close to 1.0



# $K$ and $\varepsilon$ Equations

$$\frac{\partial k}{\partial t} + U \frac{\partial k}{\partial x} + V \frac{\partial k}{\partial y} = \frac{\partial}{\partial x} \left( \frac{\nu_t}{\sigma_k} \frac{\partial k}{\partial x} \right) + \frac{\partial}{\partial y} \left( \frac{\nu_t}{\sigma_k} \frac{\partial k}{\partial y} \right) + P_h + P_{kb} + P_v - \varepsilon$$

$$\frac{\partial \varepsilon}{\partial t} + U \frac{\partial \varepsilon}{\partial x} + V \frac{\partial \varepsilon}{\partial y} = \frac{\partial}{\partial x} \left( \frac{\nu_t}{\sigma_\varepsilon} \frac{\partial \varepsilon}{\partial x} \right) + \frac{\partial}{\partial y} \left( \frac{\nu_t}{\sigma_\varepsilon} \frac{\partial \varepsilon}{\partial y} \right) + c_{\varepsilon 1} \frac{\varepsilon}{k} (P_h + c_{\varepsilon 3} P_v) + P_{\varepsilon b} - c_{\varepsilon 2} \frac{\varepsilon^2}{k}$$

New Source Term

$$P_v = \frac{c_{vk}}{\rho(1-c)} (f_{dx} U + f_{dy} V)$$

# Sediment Transport Model

## Suspended-Load Transport

$$\begin{aligned} & \frac{\partial[(1-c)hS_k]}{\partial t} + \frac{\partial[(1-c)UhS_k]}{\partial x} + \frac{\partial[(1-c)VhS_k]}{\partial y} \\ &= \frac{\partial}{\partial x} \left\{ \varepsilon_s h \frac{\partial[(1-c)S_k]}{\partial x} \right\} + \frac{\partial}{\partial y} \left\{ \varepsilon_s h \frac{\partial[(1-c)S_k]}{\partial y} \right\} + \alpha \omega_{sk} (1-c)(S_{*k} - S_k) \end{aligned}$$

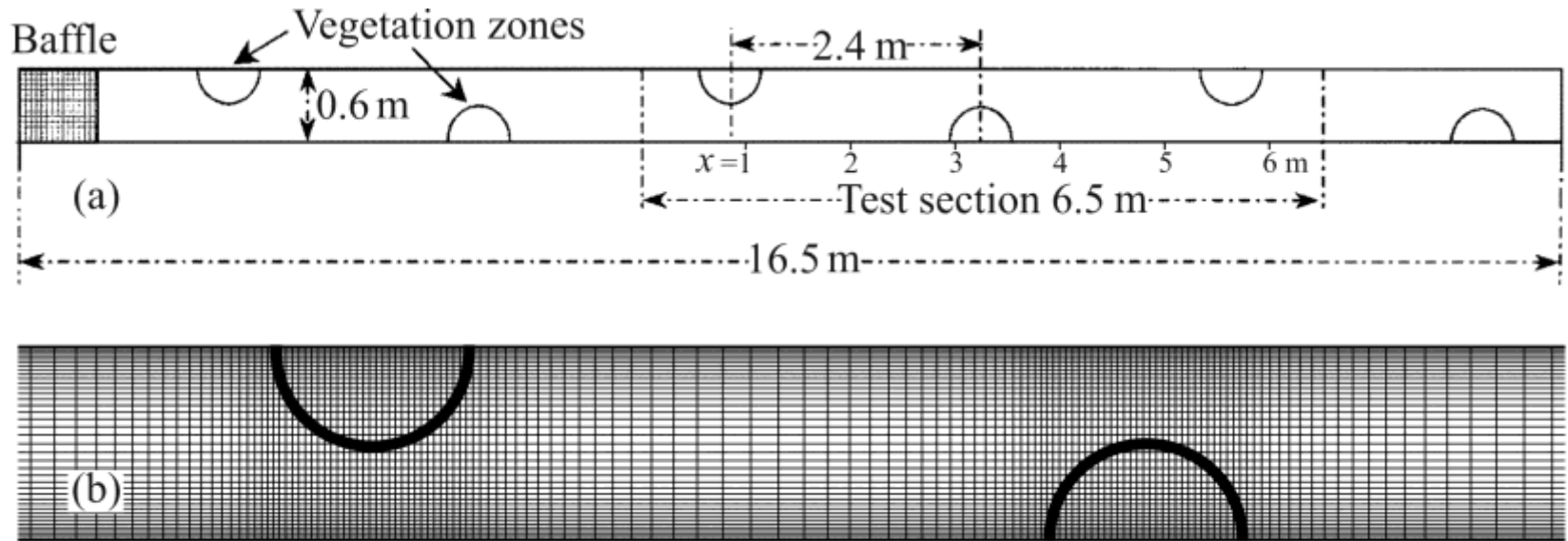
## Bed-Load Transport

$$\frac{\partial[(1-c)\delta\bar{s}_{bk}]}{\partial t} + \frac{\partial[\alpha_{bx}(1-c)q_{bk}]}{\partial x} + \frac{\partial[\alpha_{by}(1-c)q_{bk}]}{\partial y} + \frac{1}{L}(1-c)(q_{bk} - q_{b*k}) = 0$$

## Bed Change

$$(1-p') \frac{\partial z_{bk}}{\partial t} = \alpha \omega_{sk} (S_k - S_{*k}) + \frac{1}{L} (q_{bk} - q_{b*k})$$

# Flow around Alternate Vegetation Bars

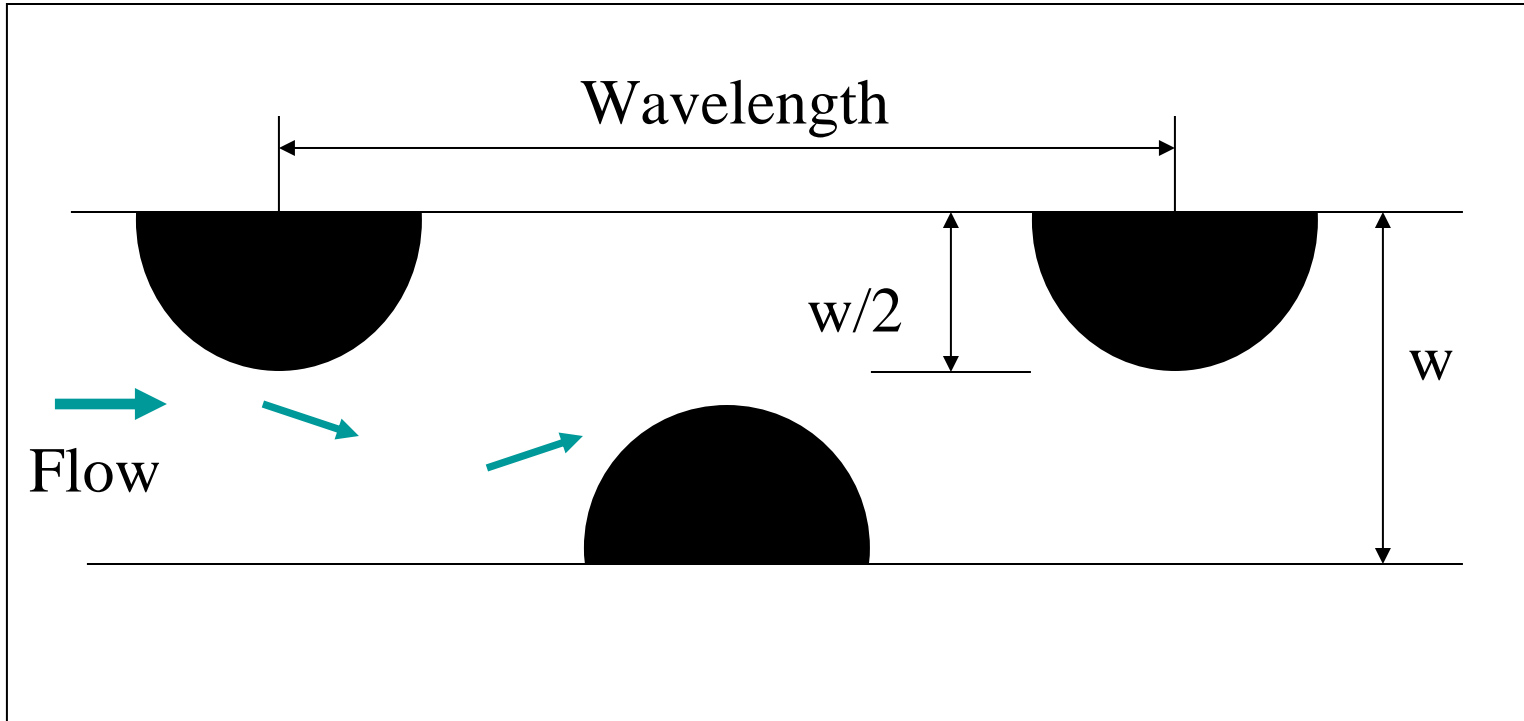


Sketch of the flume with the simulated vegetation zones  
(Bennett et al., 1999)

and computational mesh near vegetation zones



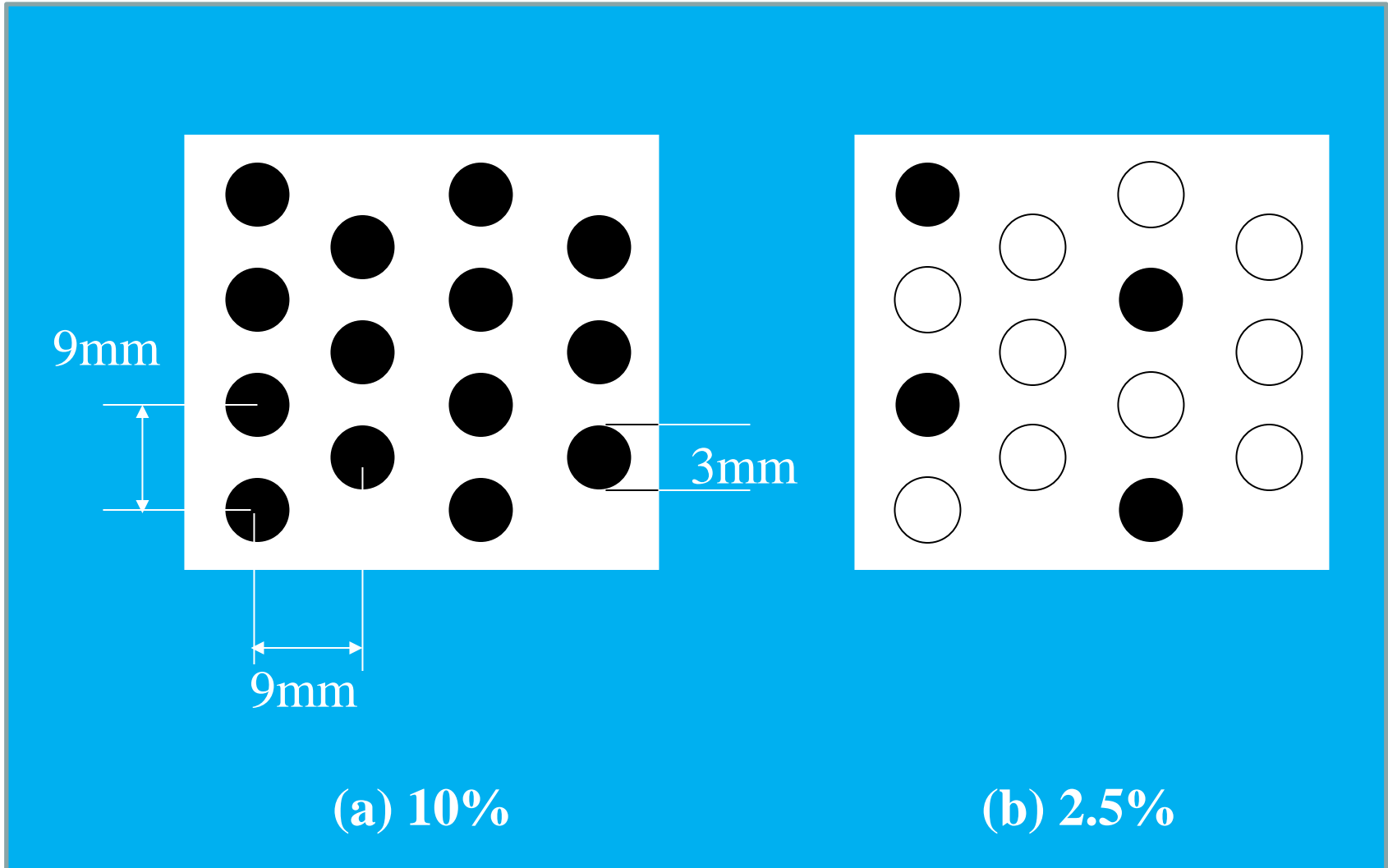
# Plan view of the flume with vegetation areas



Wavelength = 4.8 m

$w = 0.6$  m

# Close-up schematic of dowel configuration

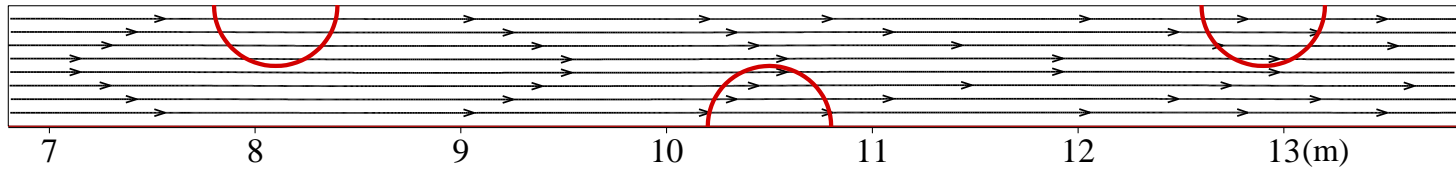


# Experiment Conditions

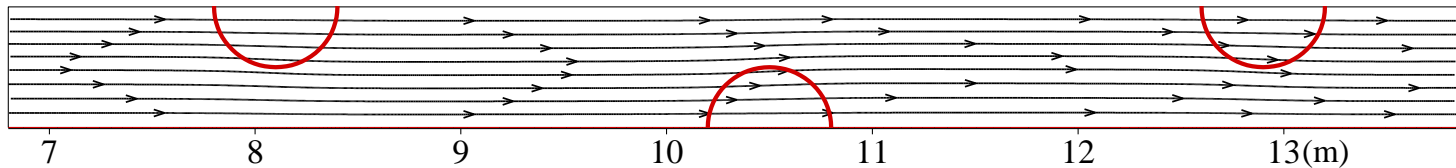
<b>Discharge (Q)</b>	<b>0.0043 m<sup>3</sup>/s</b>
<b>Depth (d)</b>	<b>27 mm</b>
<b>Width (w)</b>	<b>0.6 m</b>
<b>Froude Number (Fr)</b>	<b>0.47</b>
<b>Vegetation Density</b>	<b>10% - 0.04%</b>

# Streamlines

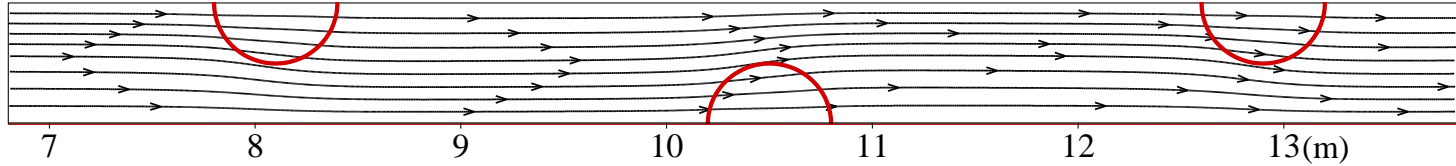
Vegetation Concentration: 0.04%



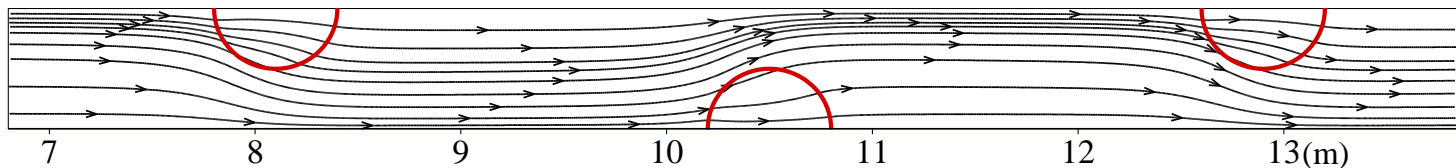
Vegetation Concentration: 0.2%



Vegetation Concentration: 0.6%

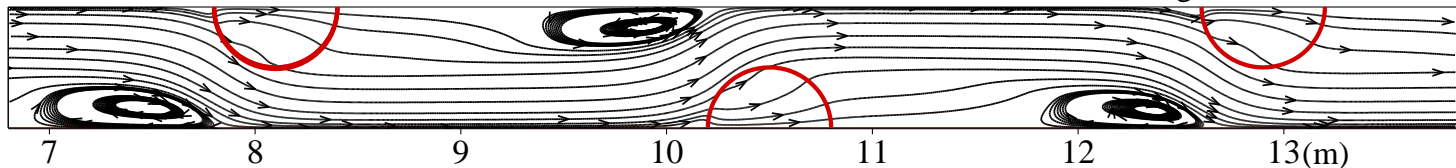


Vegetation Concentration: 2.5%



Vegetation Concentration: 10%

Vegetation Zone

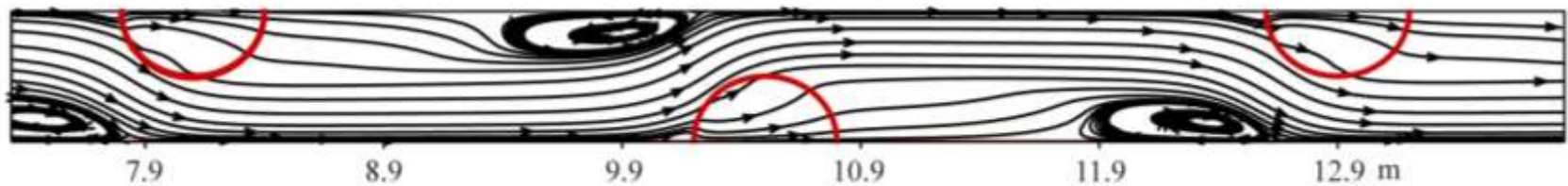


# Streamlines (Vegetation Concentration $c=10\%$ )

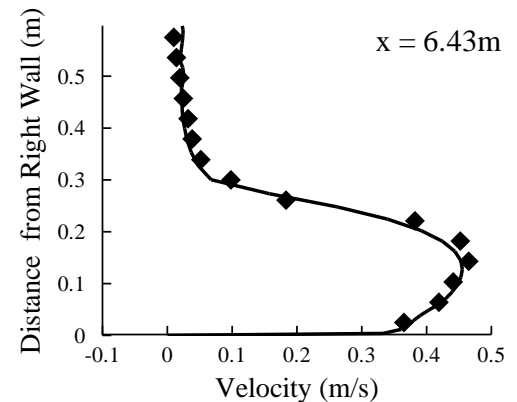
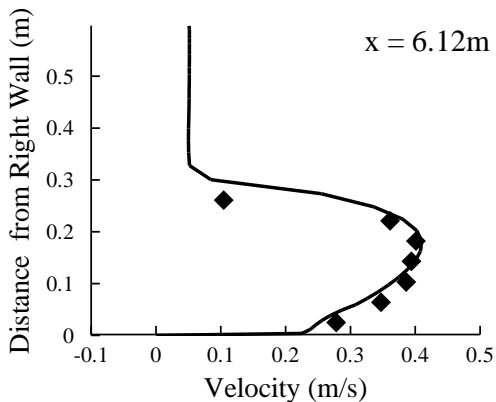
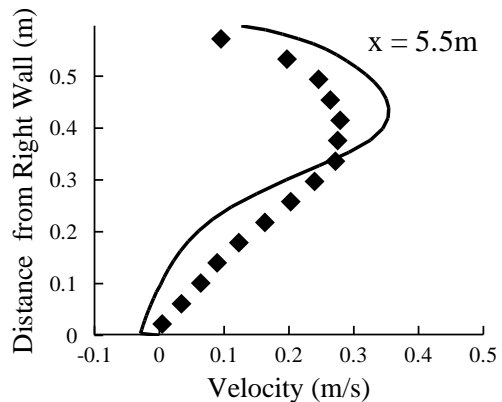
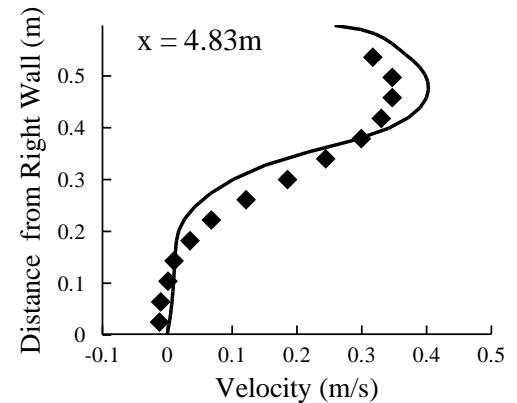
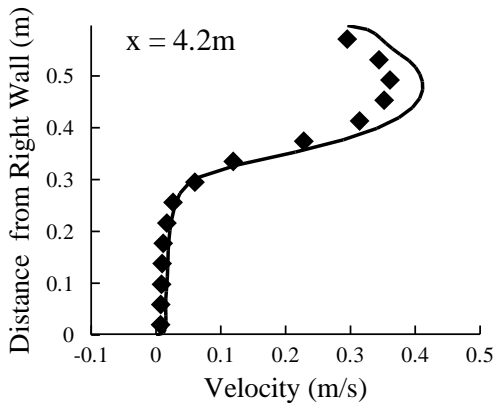
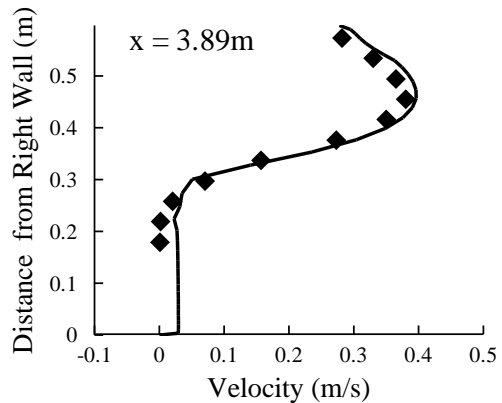
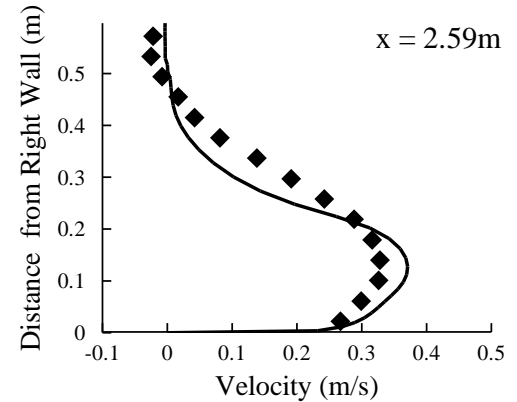
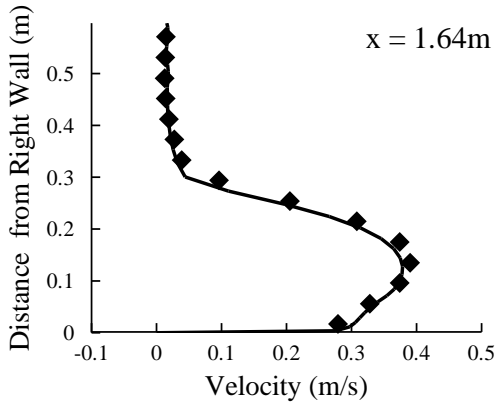
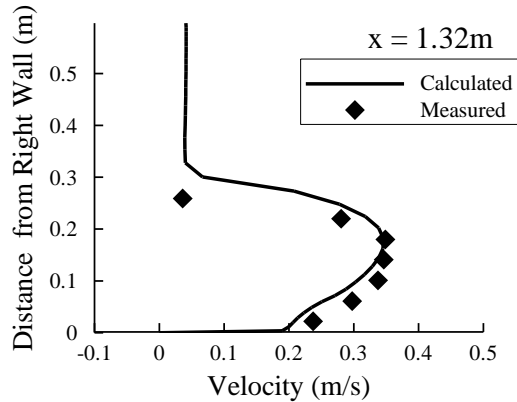
Experiment



Simulation

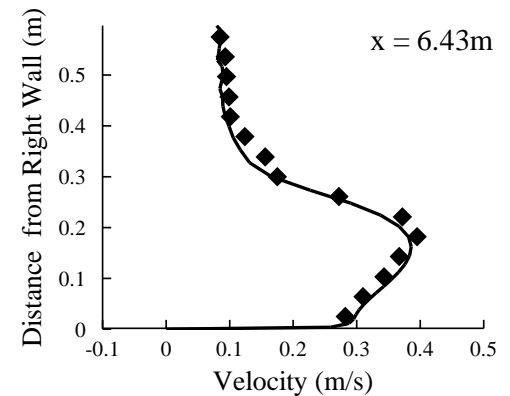
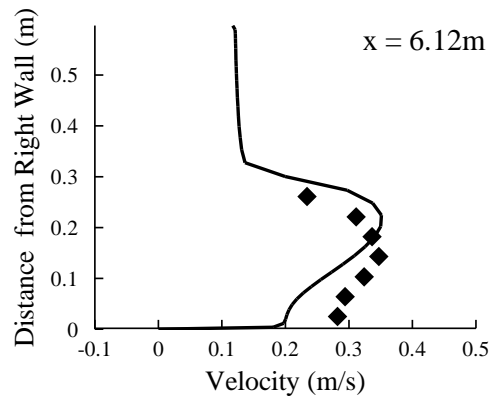
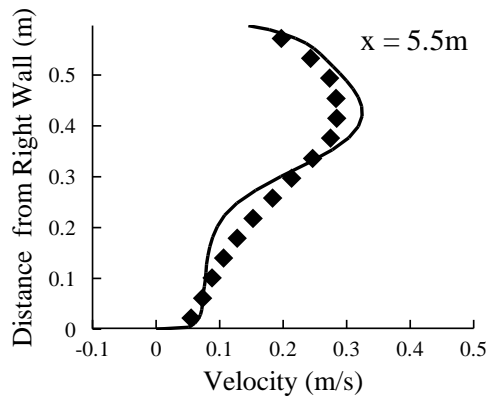
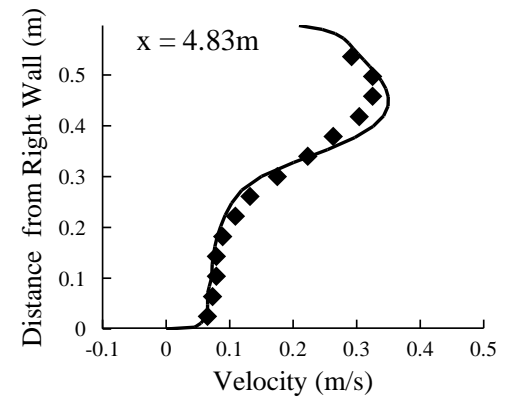
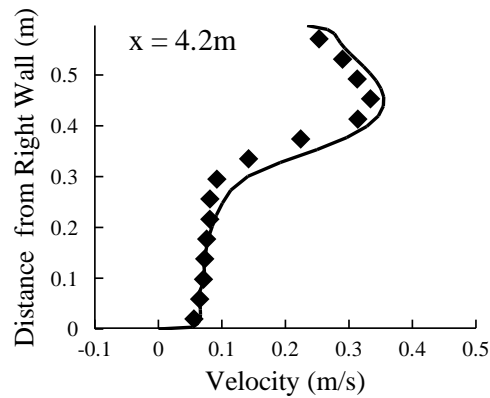
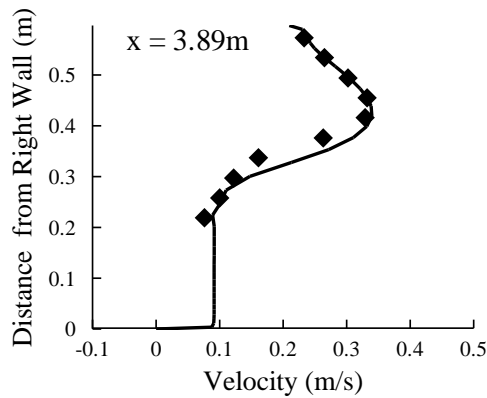
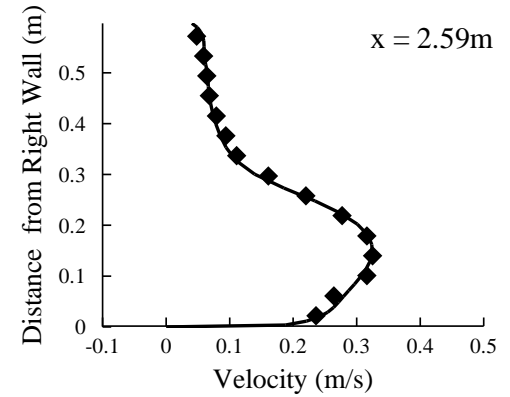
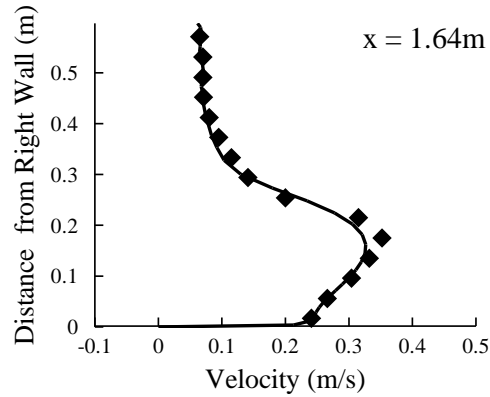
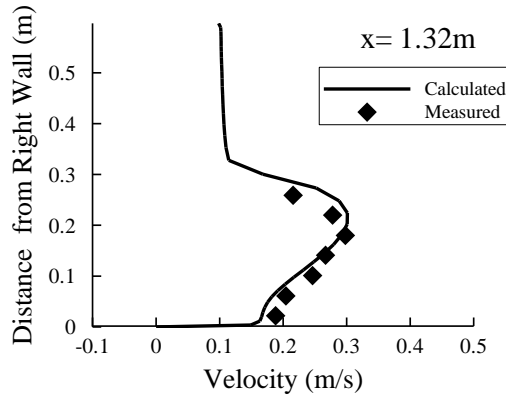


# Velocity Comparison (c=10%)

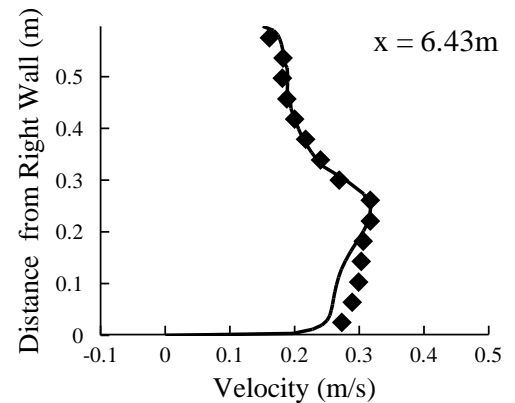
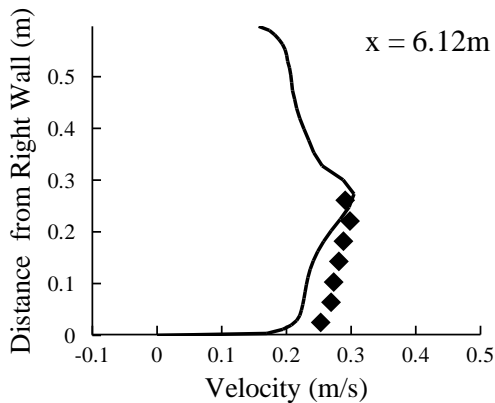
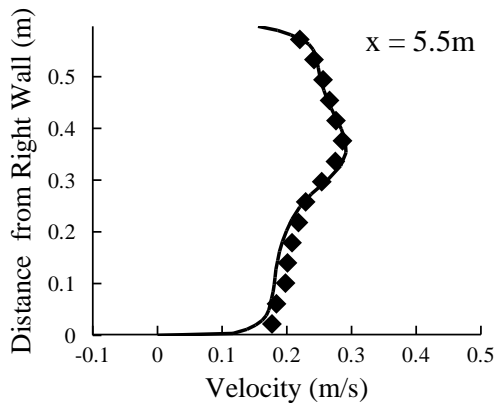
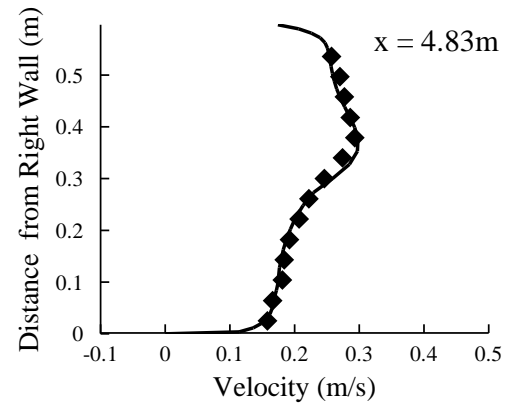
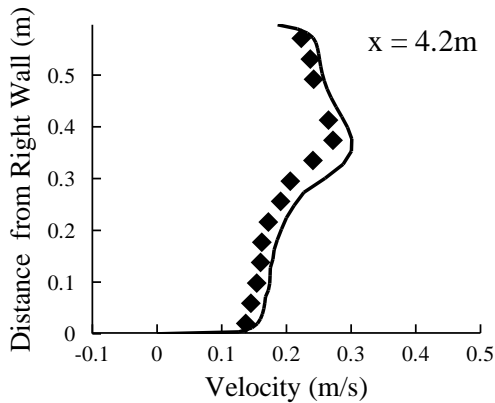
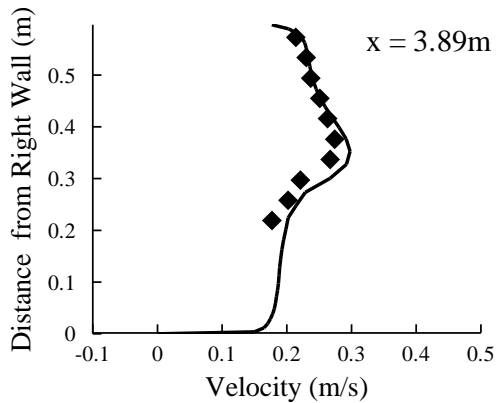
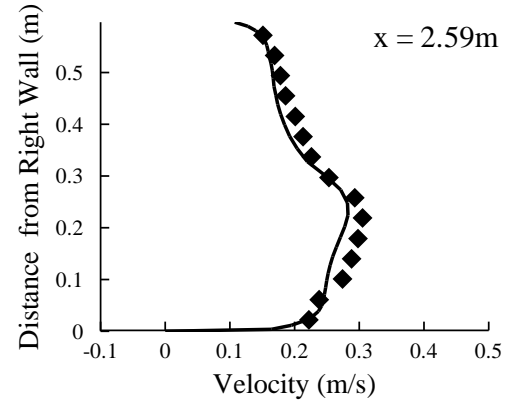
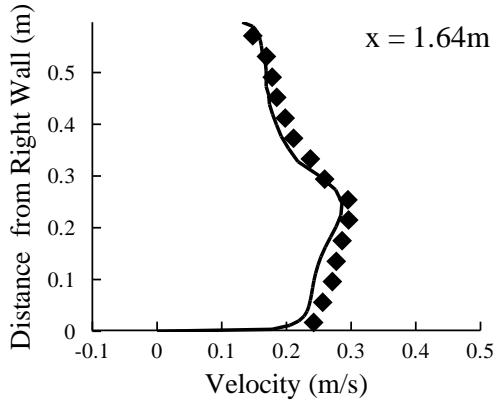
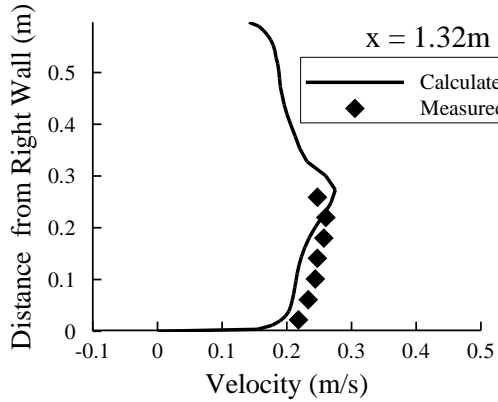




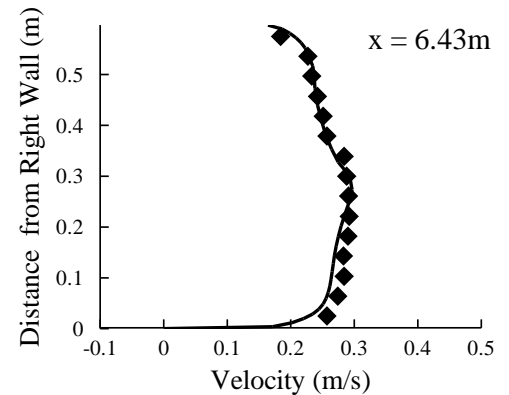
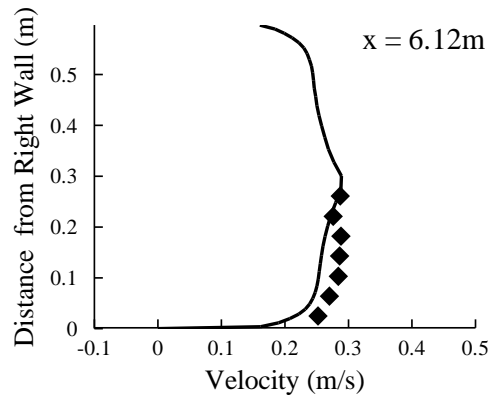
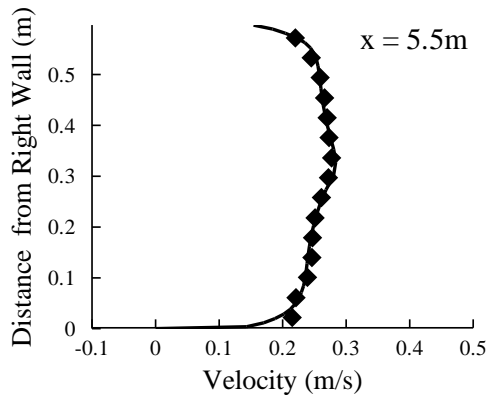
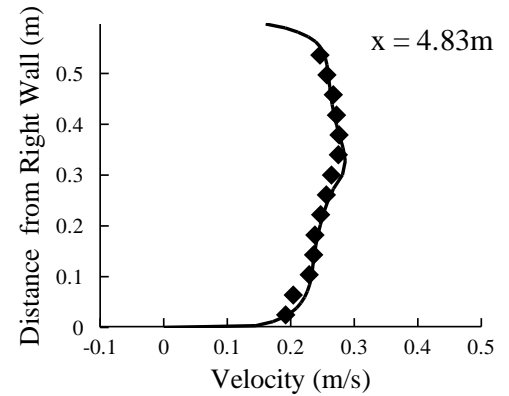
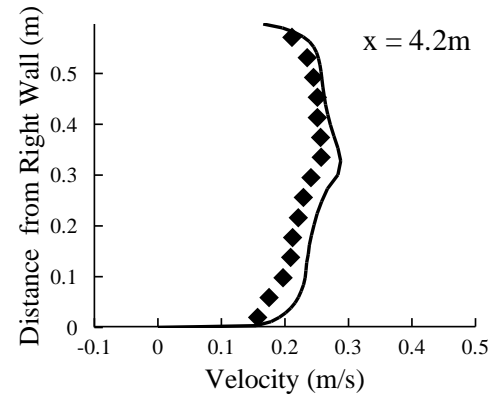
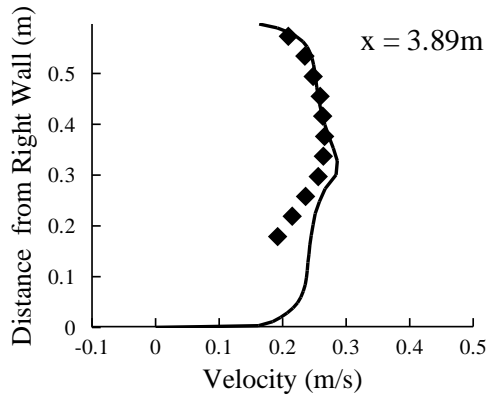
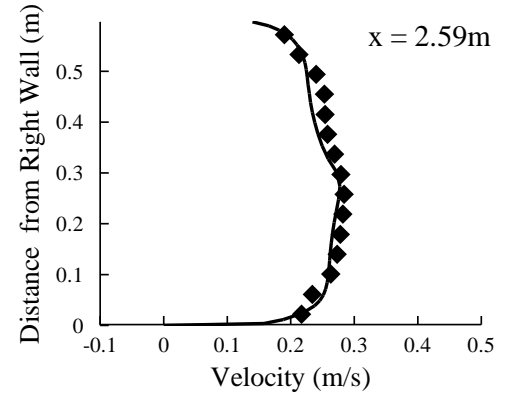
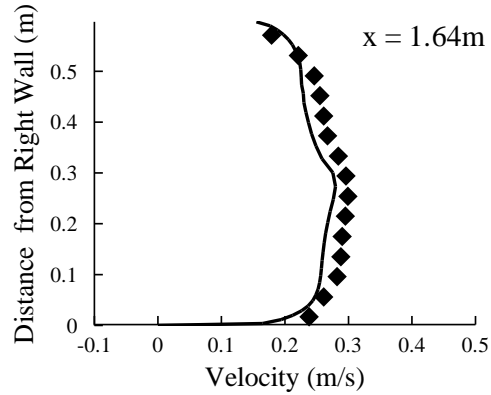
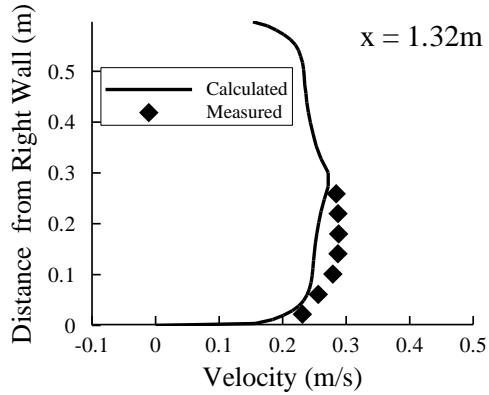
# Velocity Comparison (c=2.5%)



# Velocity Comparison (c=0.6%)



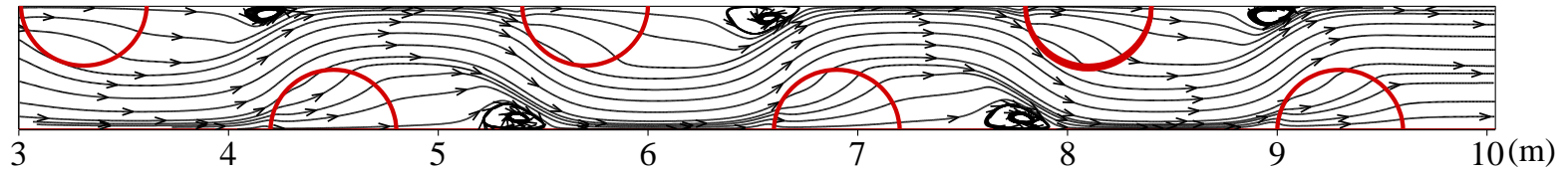
# Velocity Comparison (c=0.2%)



# Vegetation Zones with Various Wavelength

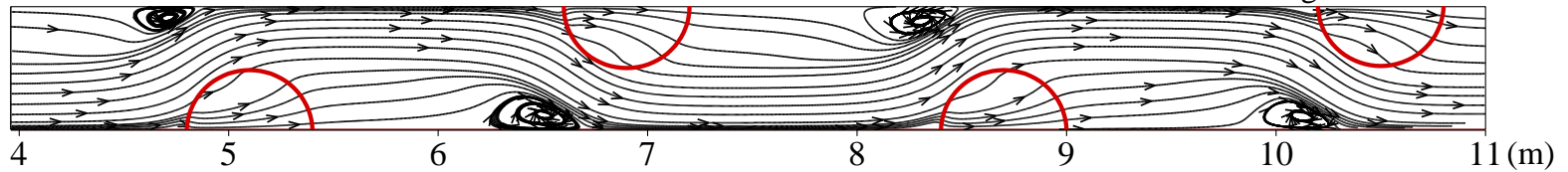
Vegetation Zone

Wavelength: 2.4 m

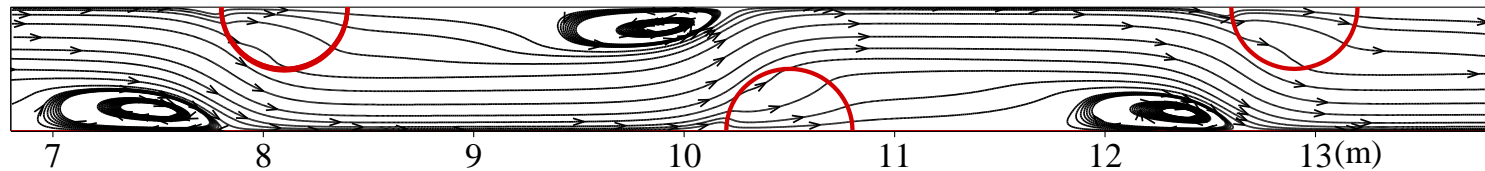


Wavelength: 3.6 m

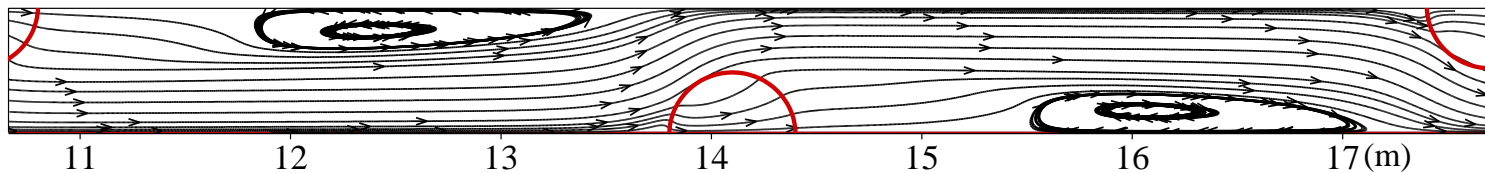
Vegetation Zone



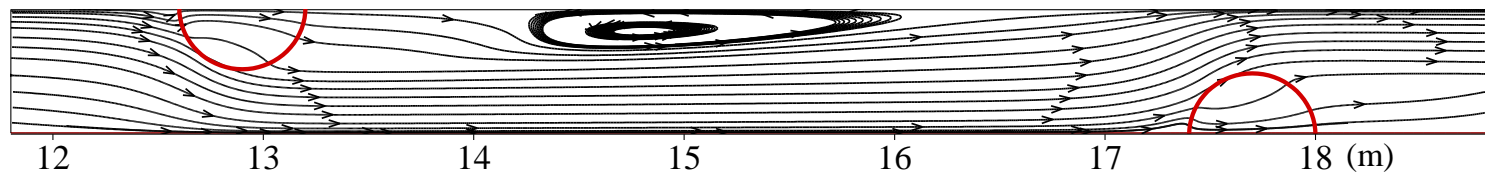
Wavelength: 4.8 m



Wavelength: 7.2 m



Wavelength: 9.6 m



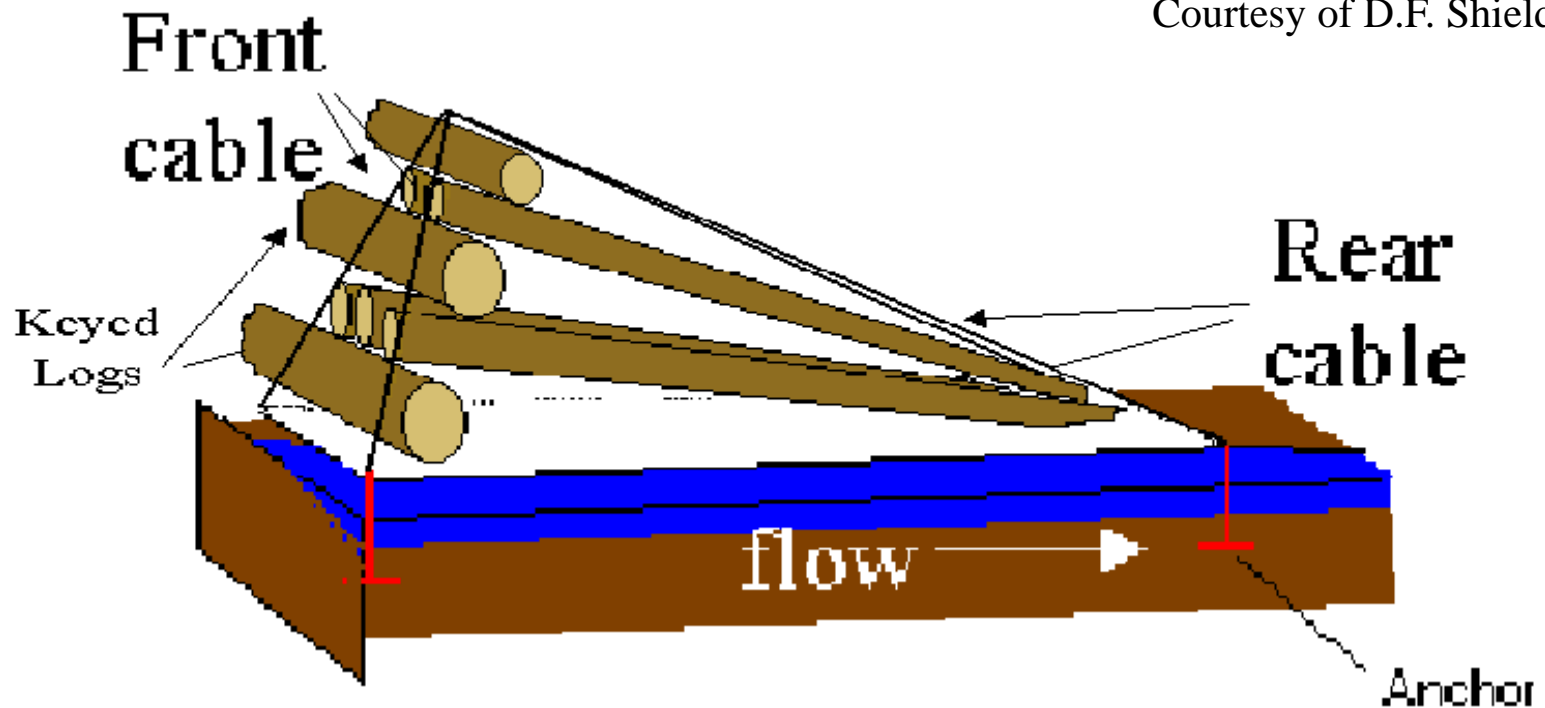
# Large Woody Structures



**A Deeply-incised Sharp Bend in Little Topashaw Creek within Yalobusha Watershed in North Central Mississippi. Installed large woody debris structures are marked in red lines.**

# Large Woody Debris Structures

Courtesy of D.F. Shields



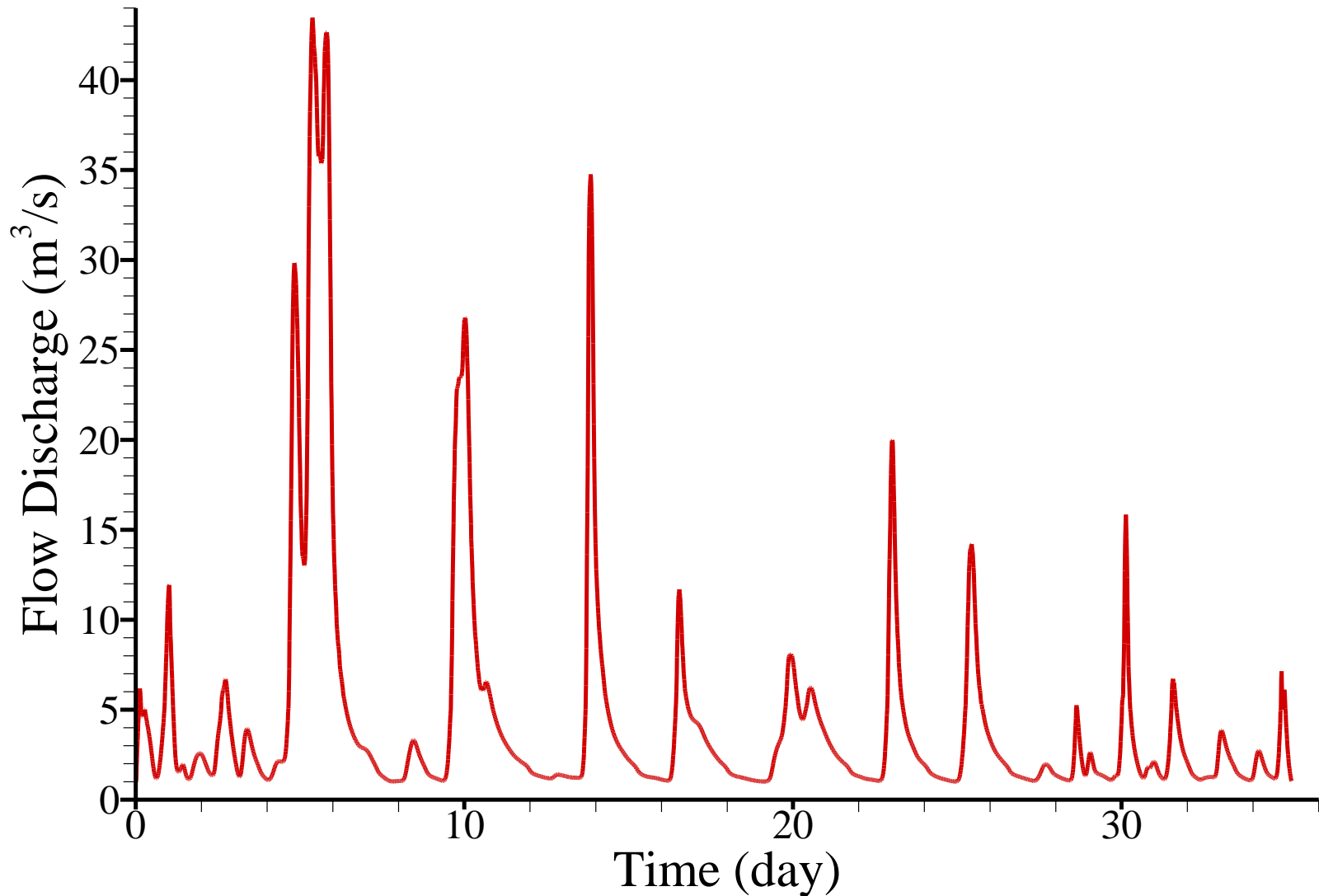
Average Diameter of Logs = 0.318 m

Average Length of Key Logs = 5.5 m

Average Length of Rack Logs = 9.2 m

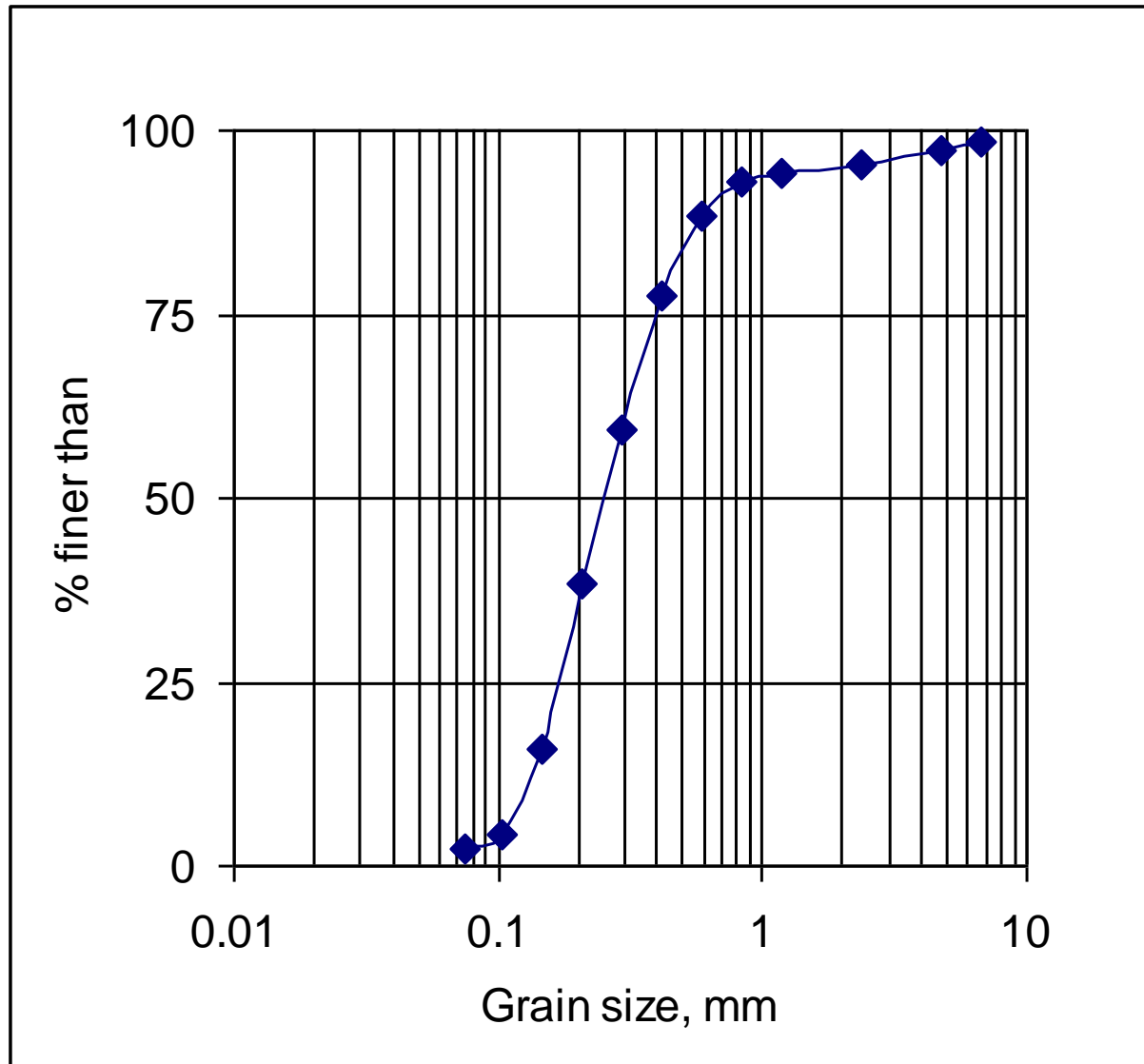


# Inflow Hydrograph (July 2000-June 2001)

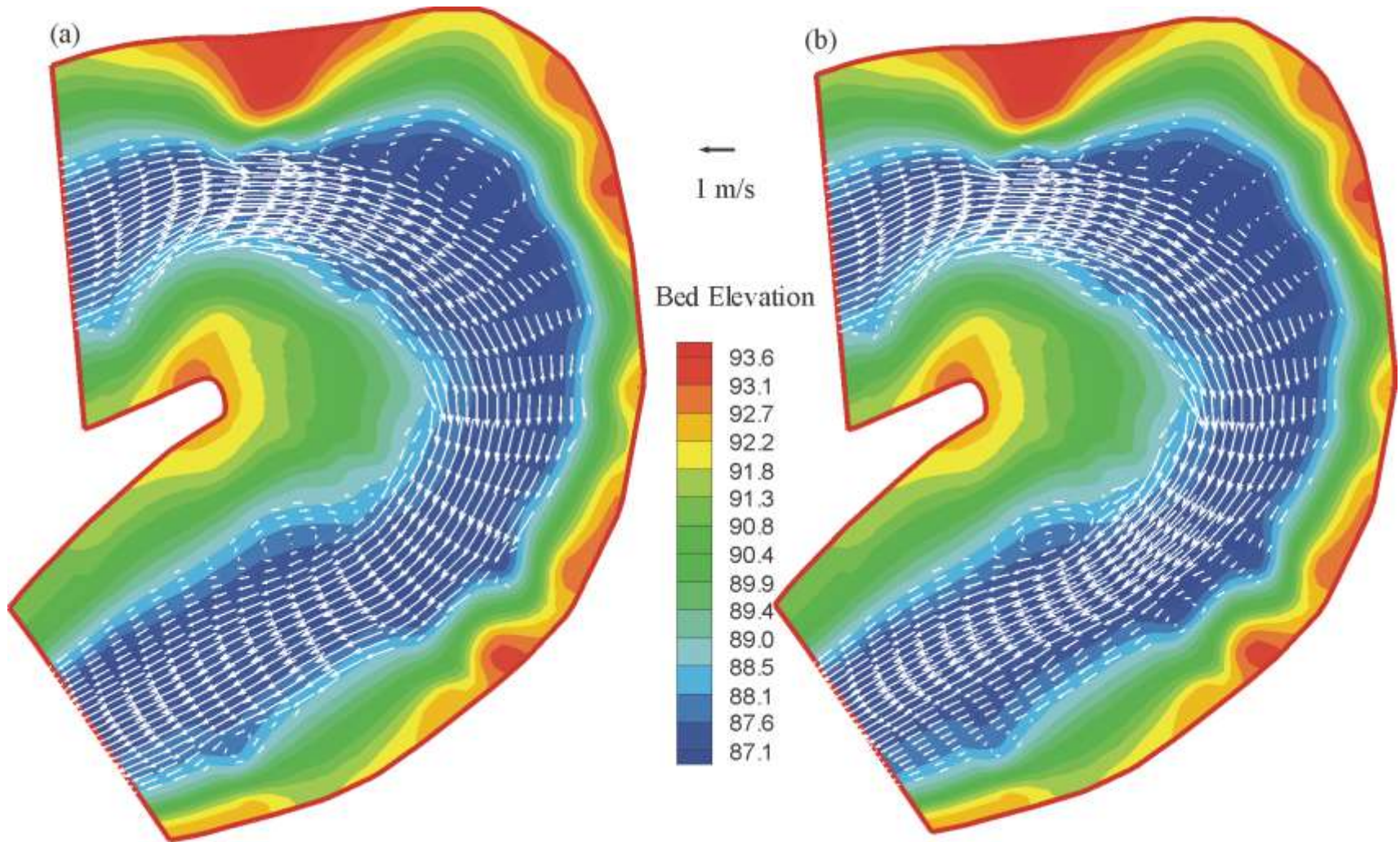


# Bed Material

$D_{84}=0.52\text{mm}$   
 $D_{50}=0.26\text{ mm}$   
 $D_{16}=0.15\text{mm}$

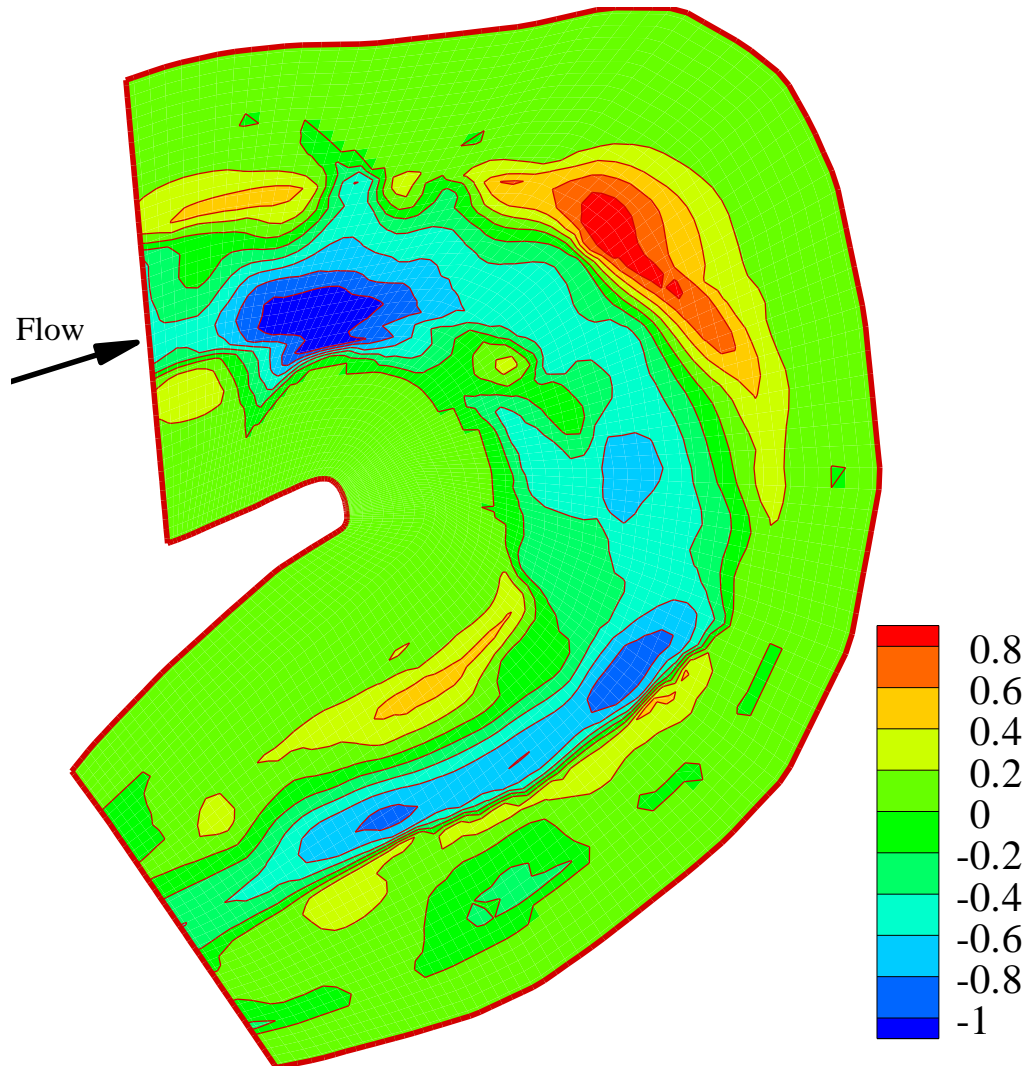


# Simulated Flows in Little Topashaw Creek

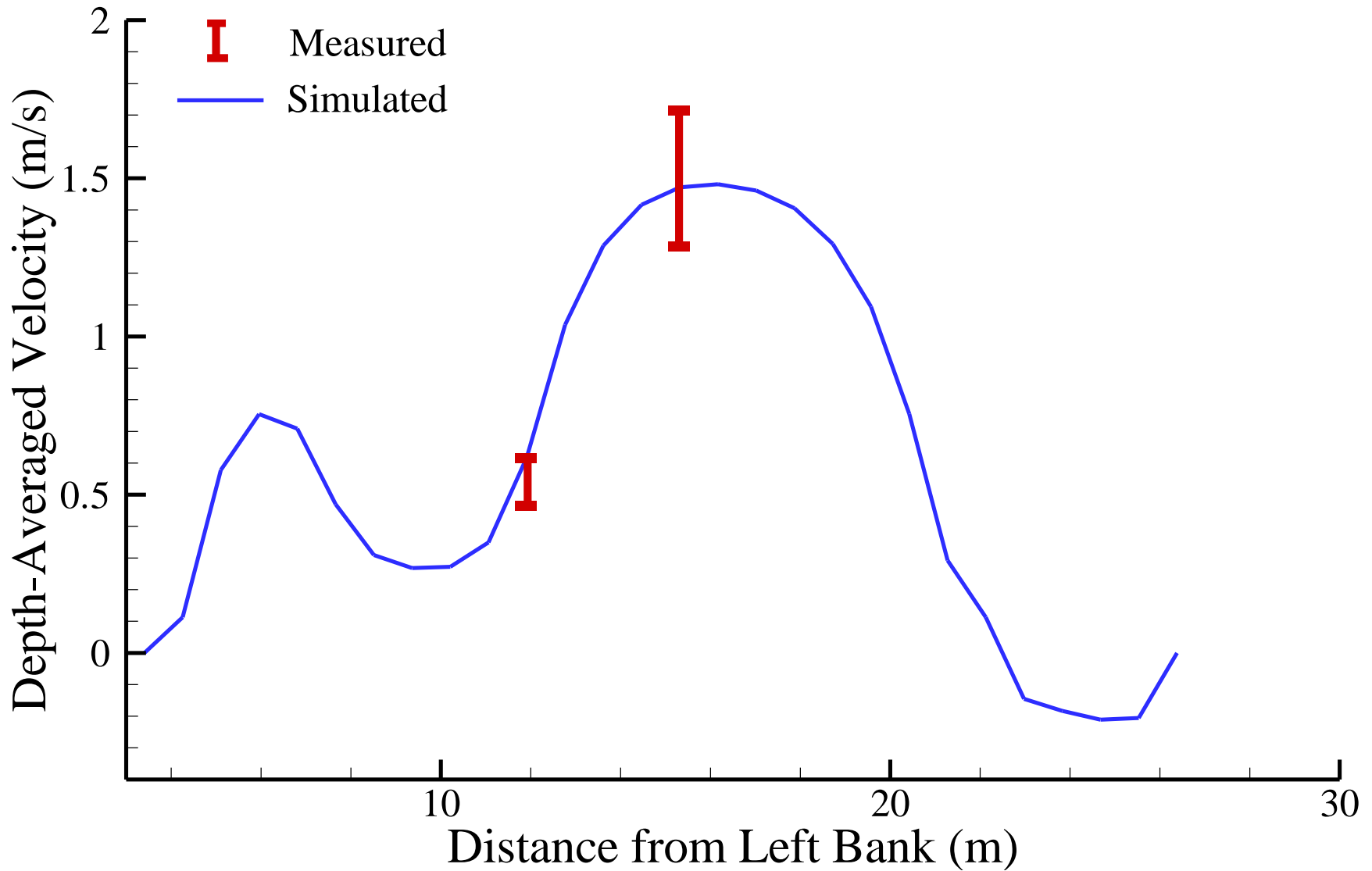


(a) without and (b) with Large Woody Structures

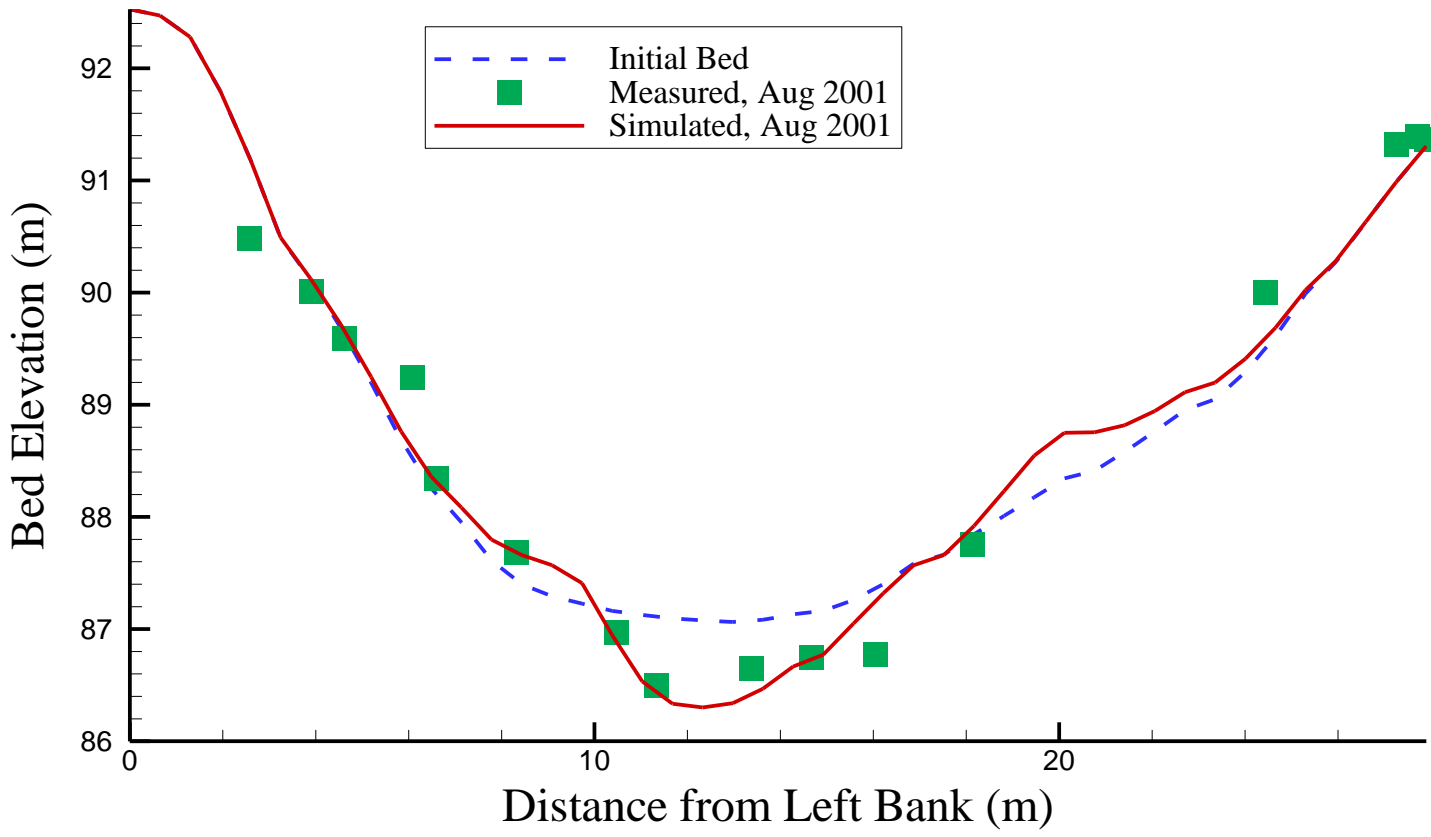
# Simulated Bed Change after 1 Year



# Flow Velocity at Cross Section LTH2



# Bed Changes after 1 Year in Cross Section LTH2





# Fish Species Considered

## **Blacktail Shiner** (*Cyprinella venusta*)



It is usually most abundant in areas with swift current and riffles with silt, gravel, and bedrock substrates.

## **Largemouth Bass** (*Micropterus salmoides*)



It is a top predator in the studied aquatic ecosystem

# Habitat Suitability Index Model

## Weighted Usable Area

$$WUA = \sum_i^M CSI_i \cdot \Delta A_i$$

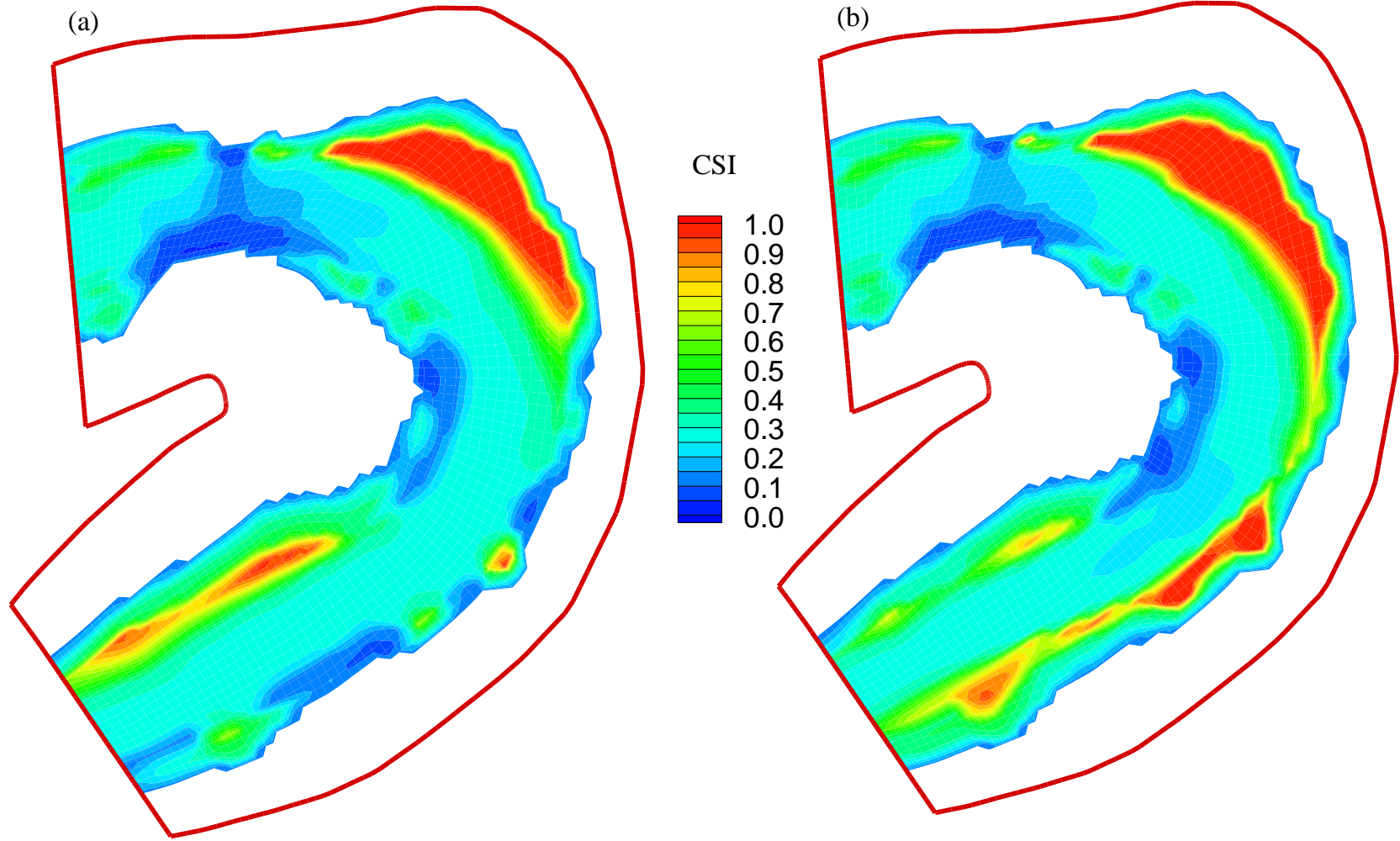
## Overall Suitability Index

$$OSI = \frac{\sum_i^M CSI_i \cdot \Delta A_i}{\sum_i^M \Delta A_i}$$

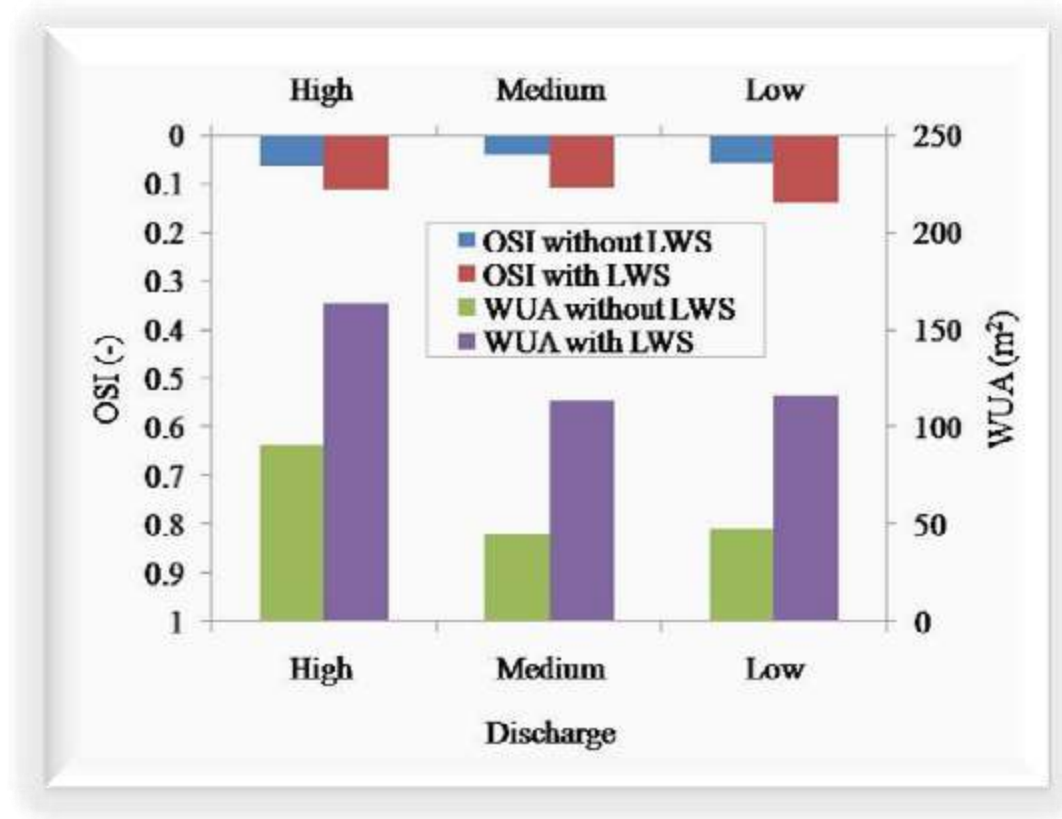
$CSI_i$  = Combined suitability index

$\Delta A_i$  = Area of each wetted cell

# Combined Habitat Suitability Index



# HSI Evaluation



The maximum increase of WUA for Blacktail Shiner was **22%**, while the maximum increase for Largemouth Bass was **155%**.

# Comparison with Observations

Discharge (m <sup>3</sup> /s)		Blacktail Shiner		Largemouth Bass	
		Weight Usable Area (m <sup>2</sup> ) Without LWS	Weight Usable Area (m <sup>2</sup> ) With LWS	Weight Usable Area (m <sup>2</sup> ) Without LWS	Weight Usable Area (m <sup>2</sup> ) With LWS
High	15.5	300.42	341.66	90.85	164.12
Medium	5.0	150.71	184.88	44.53	113.97
Low	1.5	112.97	138.35	47.26	116.15

Table 4 Summary of electrofishing catch (mean values) before and after LWS construction (Shields et al., 2006)

Quantity	Upstream	Treated reach	Downstream
	Before/After	Before/After	Before/After
Total no. of fish species	13/22	19/25	17/27
Fish catch biomass, g/150 m	262/337	150/407	168/397
Mean no. of fish per sample	74/143	129/177	141/186
Mean no. of species per sample	6.8/11.4	6.8/12.8	6.3/13.1
No. of Blacktail Shiner ( <i>Cyprinella venusta</i> )	64/230	368/778	410/753
No. of Largemouth Bass ( <i>Micropterus salmoides</i> )	0/7	0/9	3/3
Length of largest individual in each sample, cm	13/16	9/14	10/12

- ✓ The number of Blacktail Shiners doubled in the treated reach.
- ✓ Largemouth Bass were captured in the treated reach following LWS construction but not before.

# **Model of Wu and Marsooli (2012) and Wu (2013)**

# 2-D Depth-Averaged Flow Equations

$$\frac{\partial(\rho h)}{\partial t} + \frac{\partial(\rho h u)}{\partial x} + \frac{\partial(\rho h v)}{\partial y} + \rho_b \frac{\partial z_b}{\partial t} = (\rho_s - \rho_w) \left[ \frac{\partial}{\partial x} \left( \varepsilon_s h \frac{\partial C_t}{\partial x} \right) + \frac{\partial}{\partial y} \left( \varepsilon_s h \frac{\partial C_t}{\partial y} \right) \right]$$

$$\begin{aligned} & \frac{\partial}{\partial t}(\rho u h) + \frac{\partial}{\partial x}(\rho u^2 h) + \frac{\partial}{\partial y}(\rho u v h) \\ &= \frac{\partial}{\partial x} \left( \mu_t h \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left( \mu_t h \frac{\partial u}{\partial y} \right) - F_x - \rho g h \frac{\partial z_s}{\partial x} - \frac{1}{2} g h^2 \frac{\partial \rho}{\partial x} - \rho g \frac{n^2 m_b U u}{h^{1/3}} \end{aligned}$$

$$\begin{aligned} & \frac{\partial}{\partial t}(\rho v h) + \frac{\partial}{\partial x}(\rho u v h) + \frac{\partial}{\partial y}(\rho v^2 h) \\ &= \frac{\partial}{\partial x} \left( \mu_t h \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial y} \left( \mu_t h \frac{\partial v}{\partial y} \right) - F_y - \rho g h \frac{\partial z_s}{\partial y} - \frac{1}{2} g h^2 \frac{\partial \rho}{\partial y} - \rho g \frac{n^2 m_b U v}{h^{1/3}} \end{aligned}$$

# Sediment Transport Model

## Sediment Transport

$$\frac{\partial(hC_t)}{\partial t} + \frac{\partial(huC_t)}{\partial x} + \frac{\partial(hvC_t)}{\partial y} = \frac{\partial}{\partial x} \left( \varepsilon_s h \frac{\partial C_t}{\partial x} \right) + \frac{\partial}{\partial y} \left( \varepsilon_s h \frac{\partial C_t}{\partial y} \right) - \frac{1}{L} (UhC_t - m_b q_{t*})$$

## Bed Change

$$(1 - p'_m) \frac{\partial z_b}{\partial t} = \frac{1}{L} (\bar{U}hC_t - m_b q_{t*}) + \frac{\partial}{\partial x} \left[ D_s \bar{U} h r_b C_t \frac{\partial z_b}{\partial x} \right] + \frac{\partial}{\partial y} \left[ D_s \bar{U} h r_b C_t \frac{\partial z_b}{\partial y} \right]$$

## Sediment Transport Capacity $q_{t*}$

**by Wu et al. (2000) Formula**



# Other Parameters

**Eddy viscosity:**

$$\nu_t = \sqrt{(\alpha_0 U_* h)^2 + (l_h^2 |\bar{S}|)^2}$$

**Sediment adaptation length:**

$$L = \max \left\{ L_b, \frac{\bar{U}h}{\alpha\omega_s} \right\}$$

Finite volume method

Explicit algorithm – Euler scheme in time

HLL Riemann Solver for streamwise intercell fluxes and  
HLPA scheme for lateral fluxes

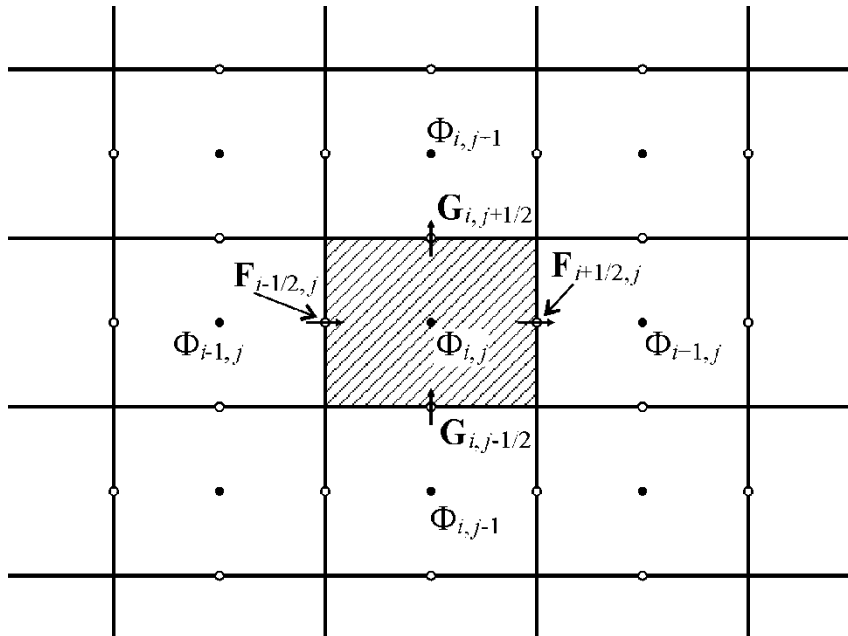
MUSCL piecewise linear reconstruction for second-order  
accuracy in space

# Finite-Volume Discretization

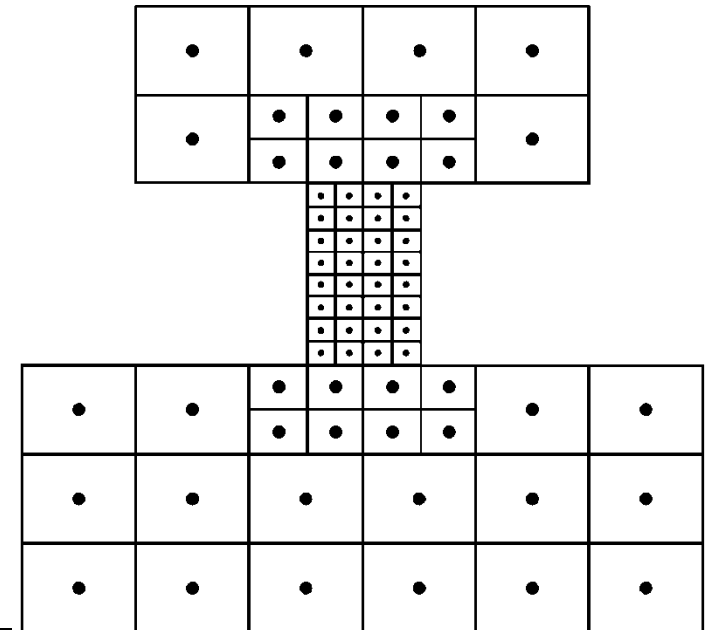
$$\frac{\partial \Phi}{\partial t} + \frac{\partial \mathbf{F}(\Phi)}{\partial x} + \frac{\partial \mathbf{G}(\Phi)}{\partial y} = \mathbf{S}(\Phi)$$

$$\Phi_{i,j}^{n+1} = \Phi_{i,j}^n - \frac{\Delta t}{\Delta x_{i,j}} \left( \mathbf{F}_{i+1/2,j}^n - \mathbf{F}_{i-1/2,j}^n \right) - \frac{\Delta t}{\Delta y_{i,j}} \left( \mathbf{G}_{i,j+1/2}^n - \mathbf{G}_{i,j-1/2}^n \right) + \Delta t \mathbf{S}_{i,j}$$

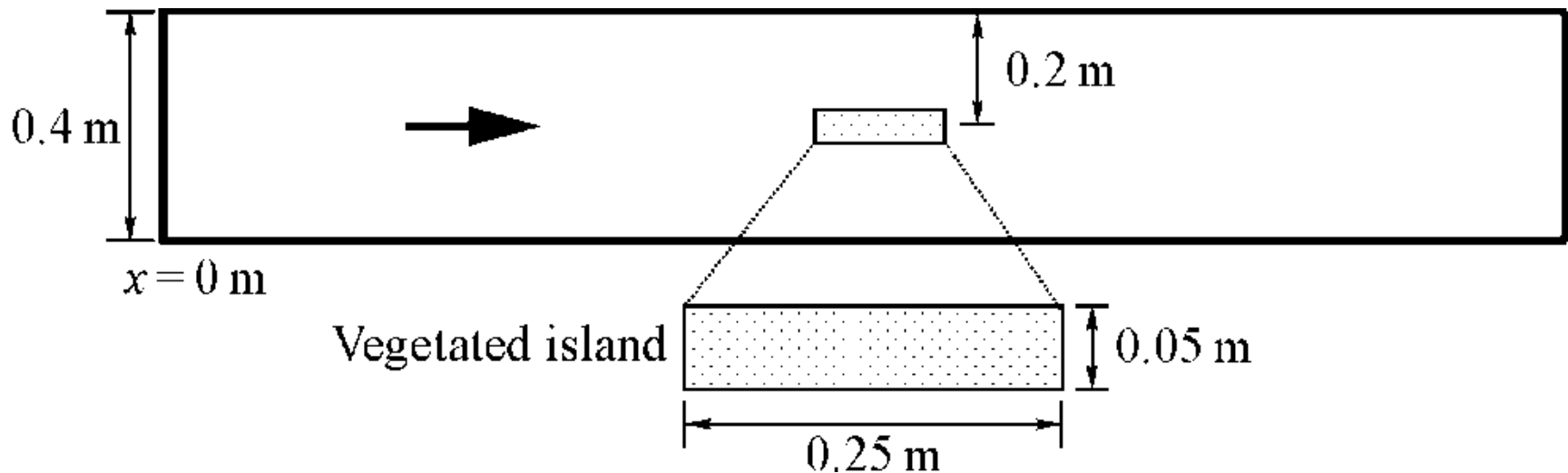
**Rectangular mesh**



**Quadtree**



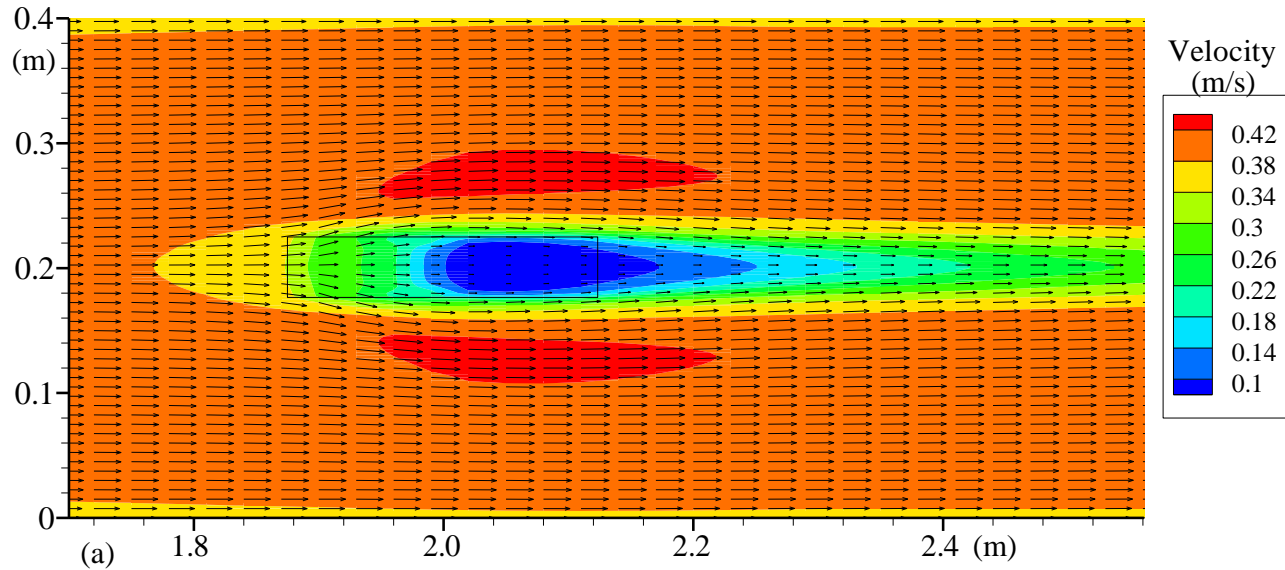
# Bed Changes around Vegetated Island



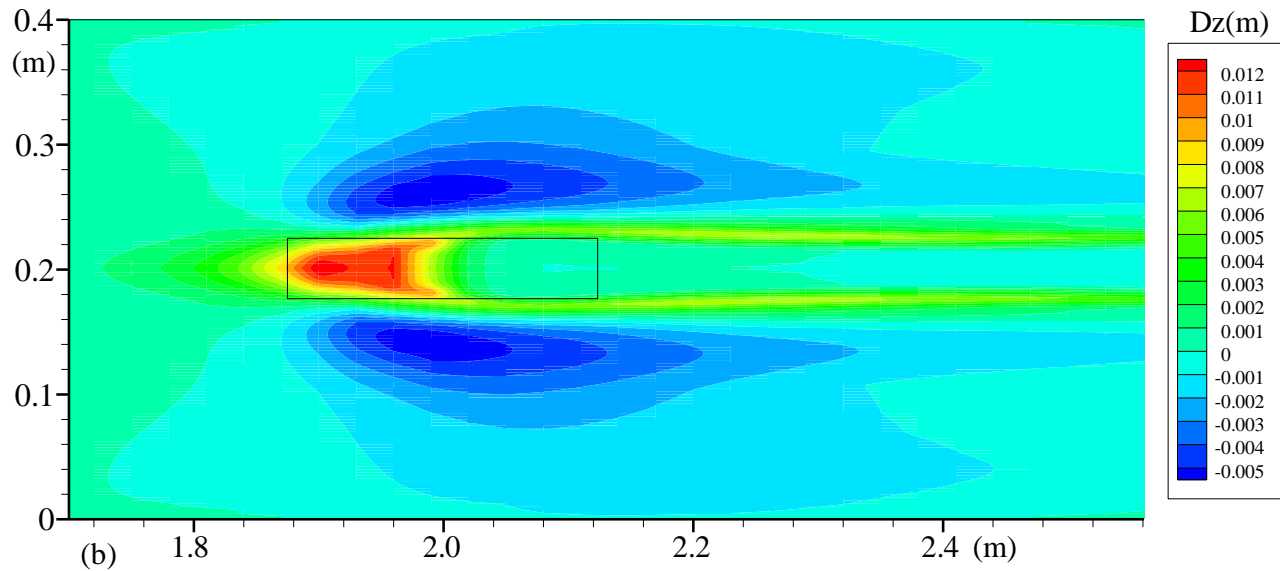
Plan view of Tsujimoto's (1998) experiments

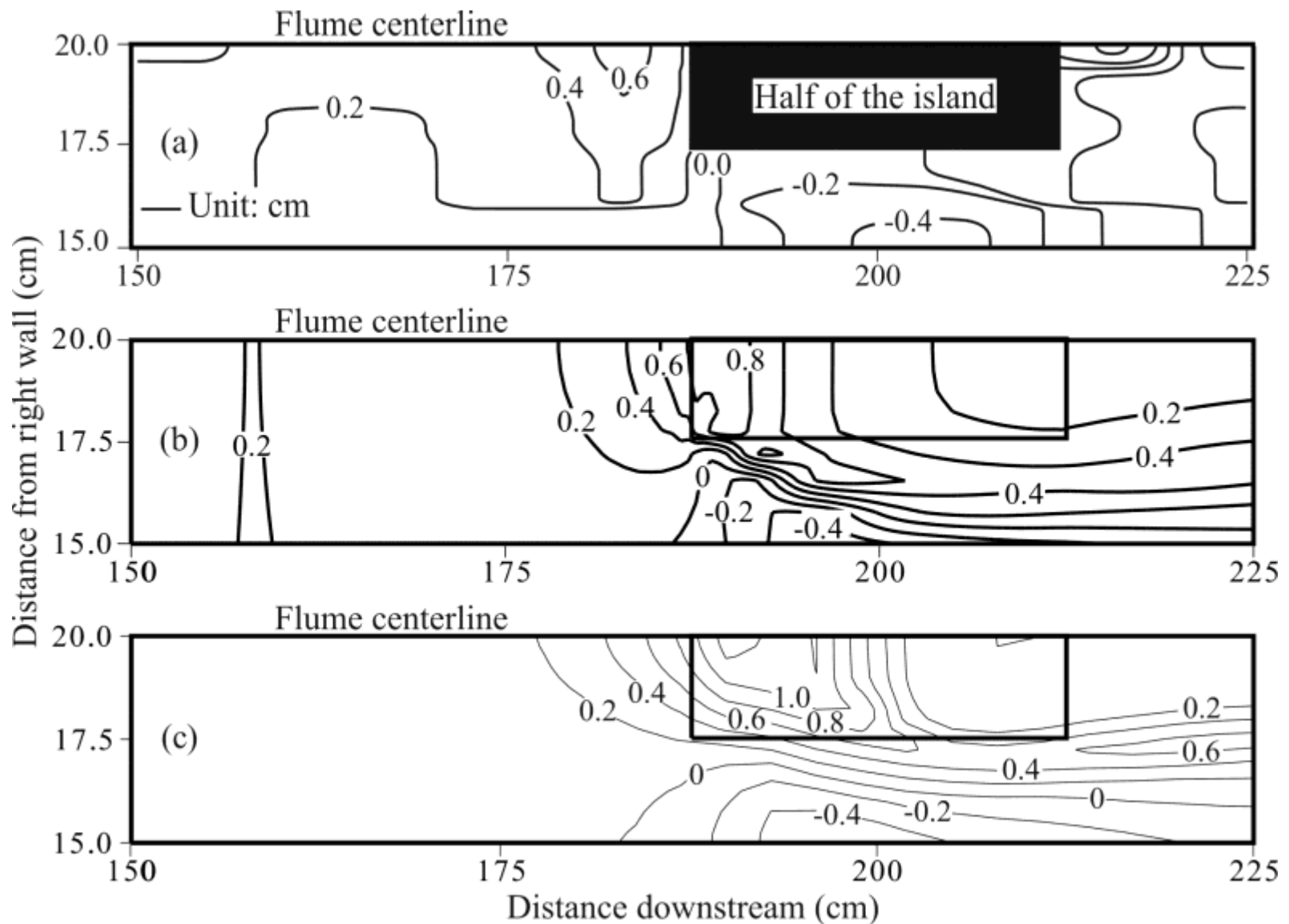
# Simulation Results (Wu, 2013)

Velocity



Bed change





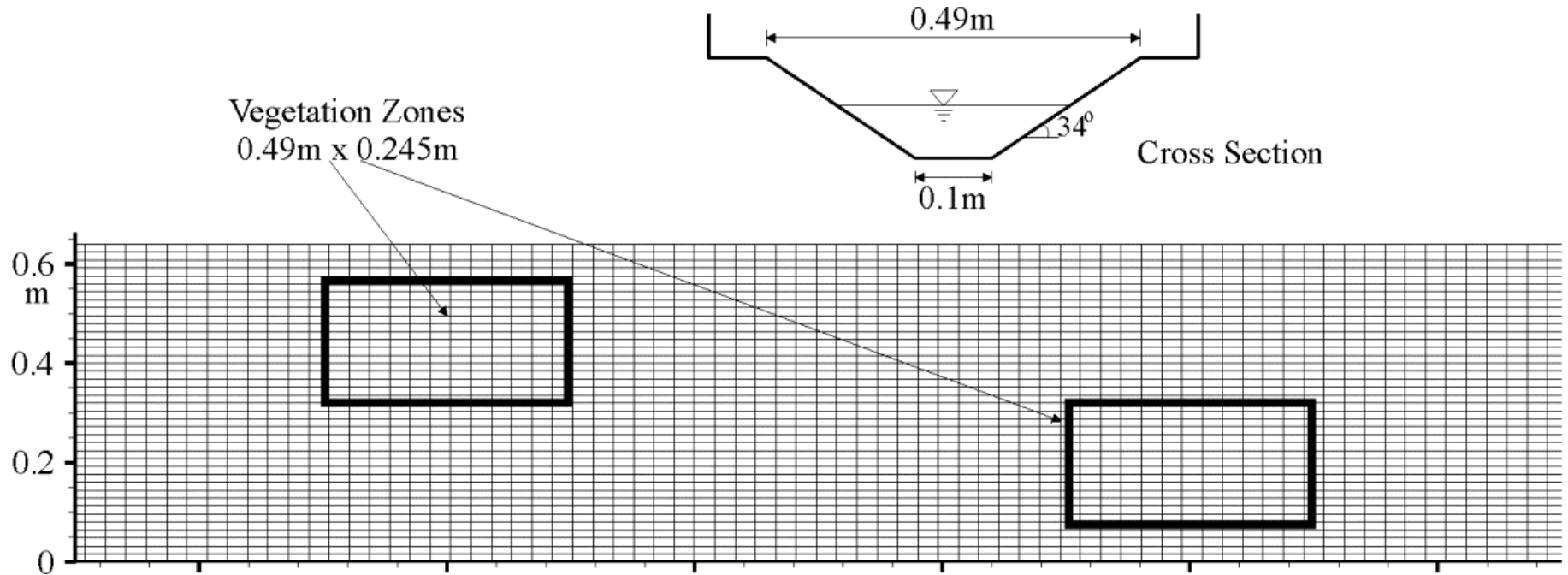
**Bed changes around vegetated island: (a) Measured by Tsujimoto (1998); (b) Calculated by Wu and Wang (2004); and (c) calculated by Wu (2013) (contour unit: cm).**

# Bed Change around Alternate Veg. Bars



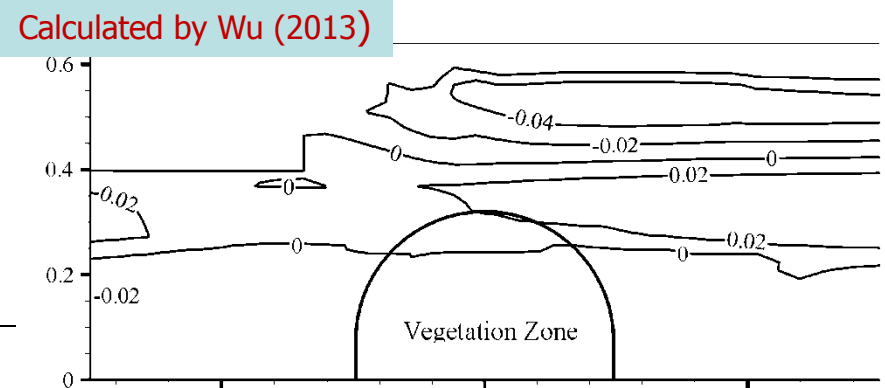
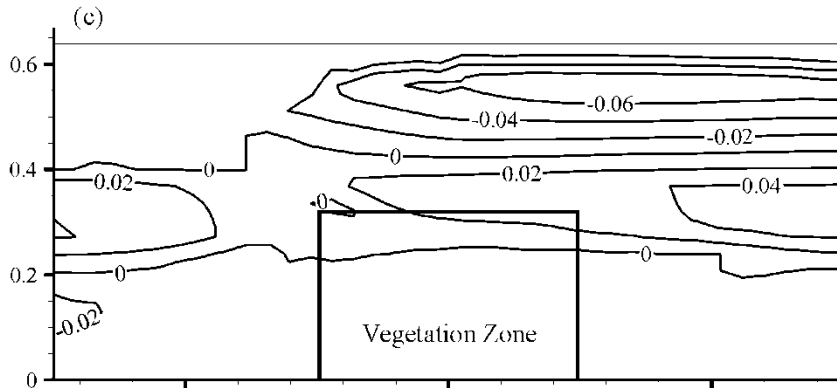
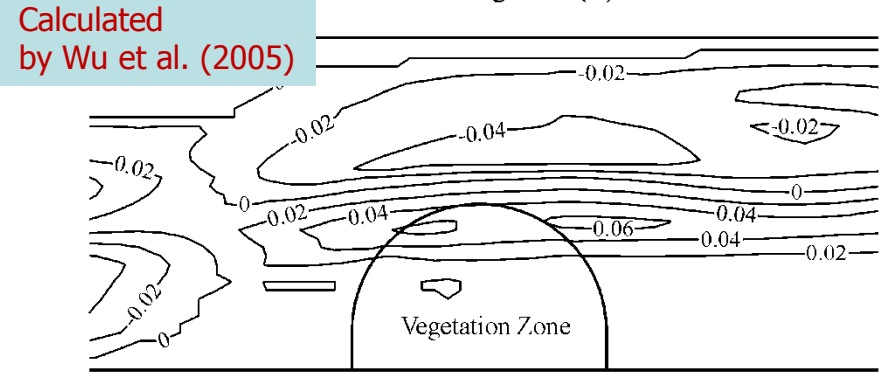
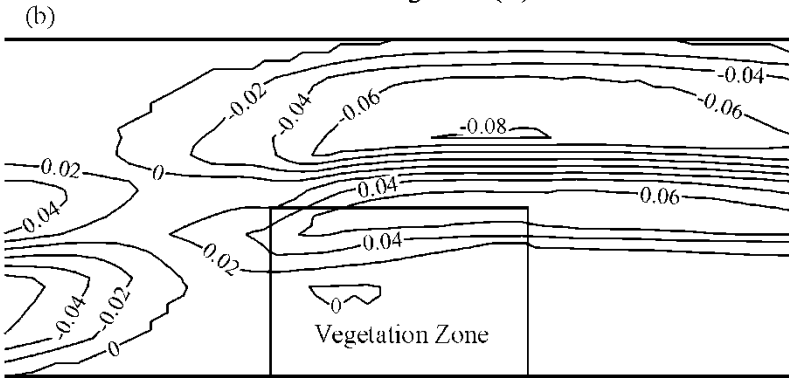
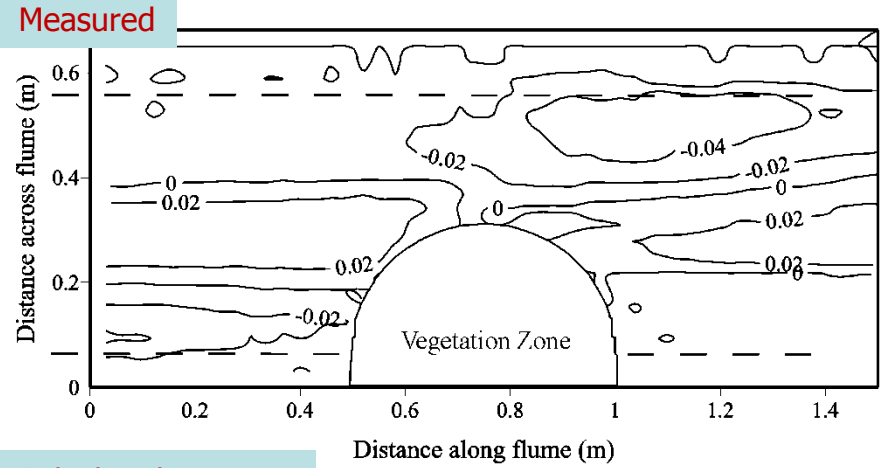
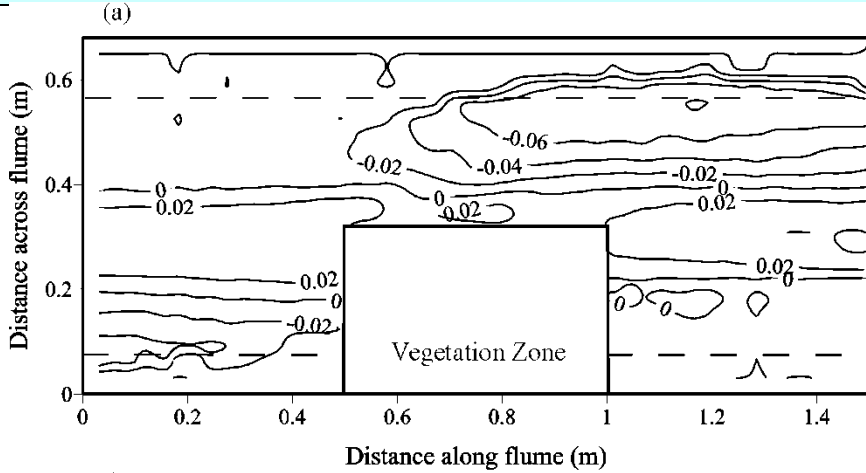
Setup of experiments of Bennett and Alonso (2003)



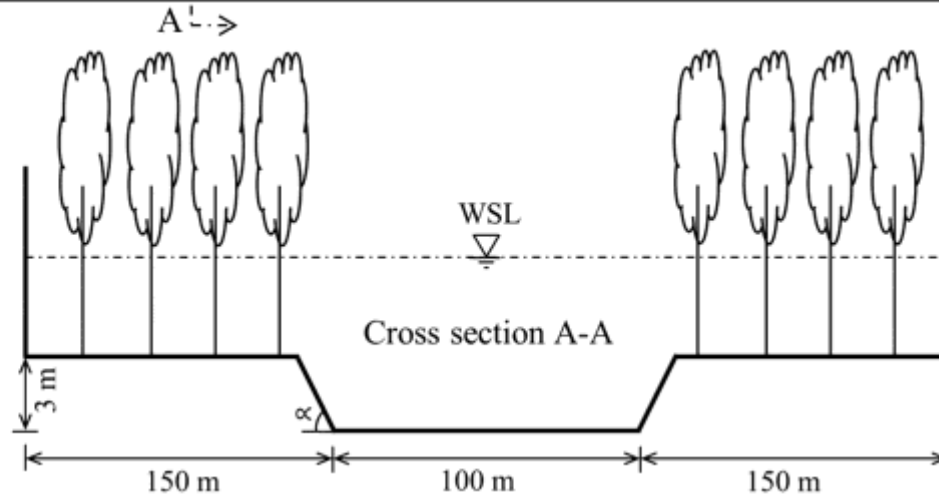
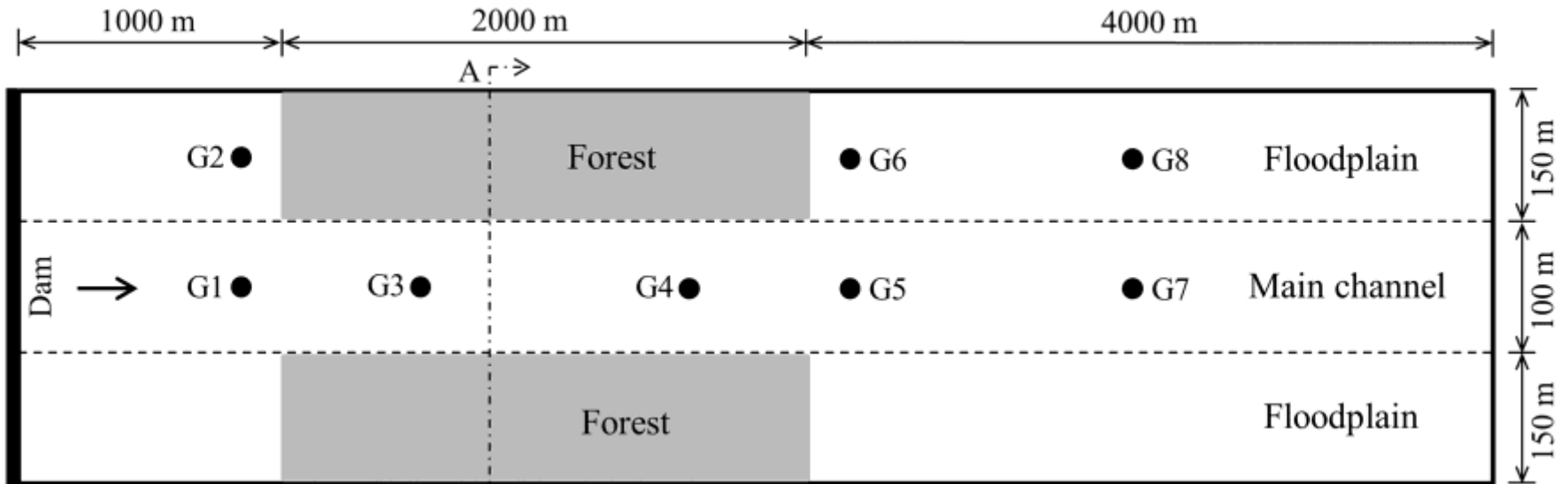


Mesh and sketch of the experiments of Bennett and Alonso (2003)

# Calculated vs. Measured Bed Changes

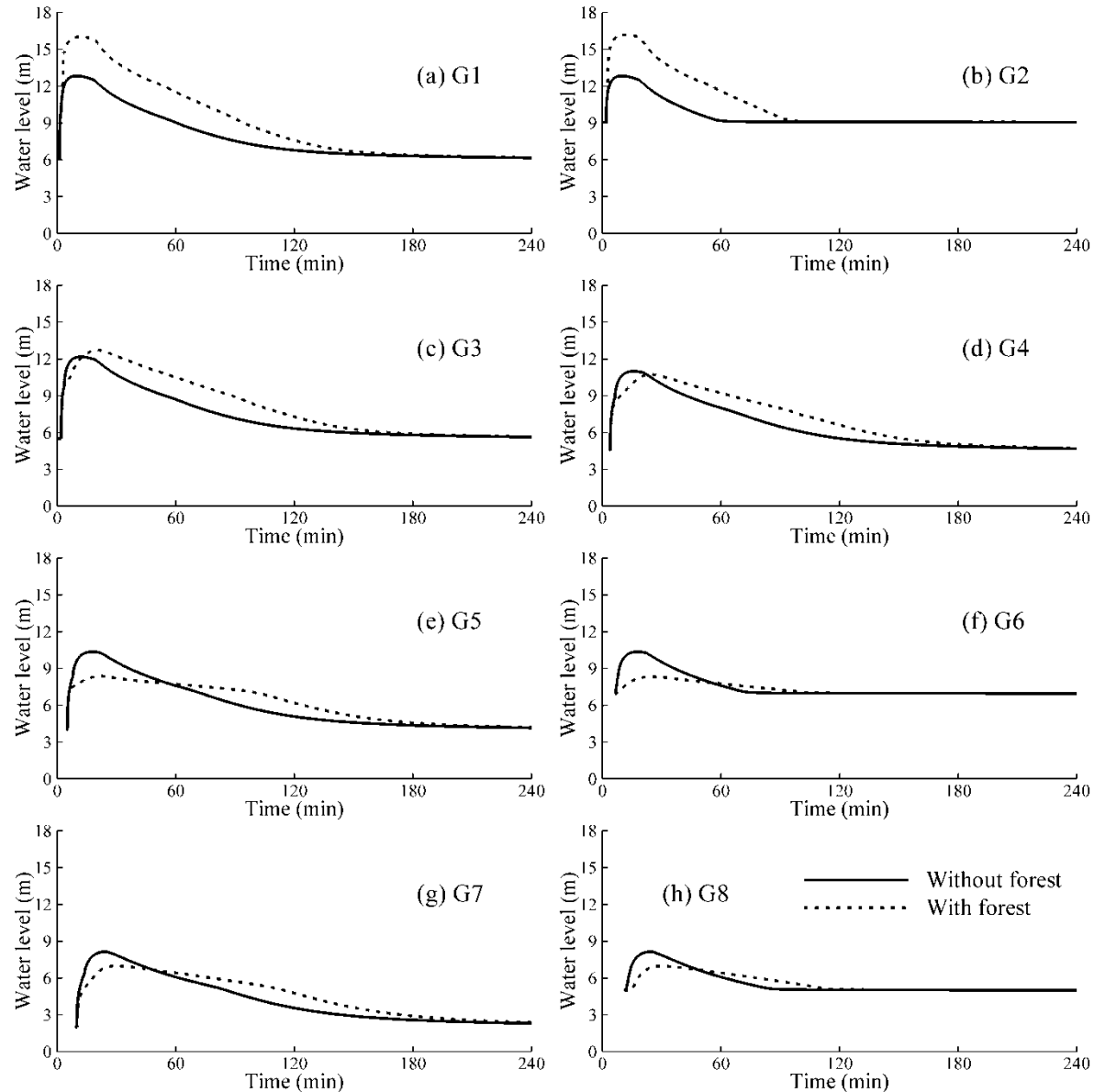


# Dam-Break Flow over Vegetated Channel



Wu and Marsooli (2012)

# Dam-Break Flow over Vegetated Channel



W. Wu and S. S.Y. Wang (2004). “Depth-averaged numerical modeling of flow and sediment transport in open channels with vegetation,” *Riparian Vegetation and Fluvial Geomorphology*, edited by S. J. Bennett and A. Simon, AGU, pp. 253–265.

W. Wu, F. D. Shields, Jr., S. J. Bennett, and S. S.Y. Wang (2005). “A depth-averaged 2-D model for flow, sediment transport and bed topography in curved channels with riparian vegetation,” *Water Resources Research*, AGU, 41(W03015), p. 15.

W. Wu (2007), *Computational River Dynamics*, Taylor & Francis, UK, 494 p.

S. J. Bennett, W. Wu, C. V. Alonso, and S. S. Y. Wang (2008). “Modeling fluvial response to in-stream woody vegetation: implications for stream corridor restoration,” *Earth Surface Processes and Landforms*, 33(6), 890–909.

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W. Wu and Z. He (2009). “Effects of vegetation on flow conveyance and sediment transport capacity,” *Int. J. Sediment Research*, 24(3), 247–259.

W. Wu and R. Marsooli (2012). “A depth-averaged 2-D shallow water model for breaking and non-breaking long waves affected by rigid vegetation.” *Journal of Hydraulic Research*, IAHR, 50(6), 558–575.

W. Wu (2013). “An explicit finite-volume depth-averaged 2-D model of morphodynamic processes near marsh edges and vegetation patches.” *Proc. 12th International Symposium on River Sedimentation*, Kyoto, Japan, Sept. 1-5.